



Ashbourne Primary School Calculation Policy (Adapted from White Rose Maths)

This policy supports the White Rose Maths scheme (Reception – Year 6) throughout the school. Progression within each area of calculation is in line with the programme of study in the 2014 National Curriculum. This calculation policy should be used to support children to develop a deep understanding of number and calculation. This policy has been designed to teach children using concrete, pictorial, and abstract representations.

Concrete representation— A pupil is first introduced to an idea or skill by acting it out with real objects. This is a ‘hands on’ component using real objects and is a foundation for conceptual understanding.

Pictorial representation – A pupil has sufficiently understood the ‘hands on’ experiences performed and can now relate them to visual representations, such as a diagram or picture of the problem.

Abstract representation—A pupil is now capable of representing problems by using mathematical notation, for example $12 \times 2 = 24$.

It is important that conceptual understanding, supported by the use of representation, is secure for all procedures. Reinforcement is achieved by going back and forth between these representations.

Our long-term aim is for children to be able to select an efficient method (whether this be mental or written) that is appropriate for a given task.

Progression of skills – Addition

Nursery	Reception	Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
-Subitise to 3 -Count how many -Make numbers to 5 -Add 1 more (through songs and rhymes)	-Conceptually subitise to 5 -1 more -Notice the composition of numbers within 10 -Combine 2 groups -Add more	-Add together -Add more -Bonds within 10 -Related facts within 20 -Missing numbers	-Add 1s to any number (related facts) -Add three 1-digit numbers -Add across a 10 -Add multiples of 10 -Add 10s to any number -Add two 2-digit numbers (not across a ten) -Add two 2-digit numbers (across a ten) -Missing numbers	-Add 1s, 10s and 100s to a 3-digit number -Add two numbers (no exchange) -Add two numbers across a 10 or 100 -Complements to 100 -Add fractions with the same denominator within 1 whole -Calculate the duration of events	-Add 1s, 10s and 100s to a 4-digit number -Add up to two 4-digit numbers -Add decimal numbers in the context of money -Add fractions and mixed numbers with the same denominator beyond 1 whole	-Add using mental strategies -Add whole numbers with more than 4 digits -Add decimals with up to 2 decimal places -Complements to 1 -Add fractions with denominators that are a multiple of one another	-Add integers up to 10 million -Add decimals with up to 3 decimal places -Order of operations -Negative numbers -Add fractions

Progression of skills – Subtraction

Nursery	Reception	Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
-Subitise to 3 -Count how many -Make numbers to 5 -Take 1 away (through songs and rhymes)	-Conceptually subitise to 5 -1 less -Notice the composition of numbers within 10 -Partition -Take away	-Find a part -Take away -Bonds within 10 -Related facts within 20 -Missing numbers	-Subtract 1s from any number (related facts) -Subtract across a 10 -Subtract multiples of 10 -Subtract 10s from any number -Subtract two 2-digit numbers (not across a ten) -Subtract two 2-digit numbers (across a ten) -Missing numbers	-Subtract 1s, 10s and 100s from a 3-digit number -Subtract two numbers (no exchange) -Subtract two numbers across a 10 or 100 -Complements to 100 -Subtract fractions with the same denominator within 1 whole	-Subtract 1s, 10s, 100s and 1,000s from a 4-digit number -Subtract up to two 4-digit numbers -Subtract decimal numbers in the context of money -Subtract fractions and mixed numbers with the same denominator	-Subtract whole numbers with more than 4 digits -Subtract using mental strategies -Subtract decimals with up to 2 decimal places -Complements to 1 -Subtract fractions with denominators that are a multiple of one another	-Subtract integers up to 10 million -Subtract decimals with up to 3 decimal places -Order of operations -Negative numbers -Subtract fractions

Progression of skills – Multiplication

Nursery	Reception	Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
-Continue with counting and subitising skills as a foundation for later work on equal groups. (see addition and subtraction sections)	-Double to 10 -Make equal groups	-Count in 2s, 5s and 10s -Add equal groups -Make arrays -Make doubles	-Link repeated addition and multiplication -Use arrays -Double -The 2 times-table -The 10 times-table -The 5 times-table -Missing numbers	-The 3 times-table -The 4 times-table -The 8 times-table -Related facts -Multiply a 2-digit number by a 1-digit number - no exchange -Multiply a 2-digit number by a 1-digit number - with exchange -Scaling -Correspondence problems	-Times-table facts to 12×12 -Multiply by 1 and 0 -Multiply 3 numbers -Factor pairs -Multiply by 10 and 100 -Related facts -Mental strategies -Multiply a 2 or 3-digit number by a 1-digit number -Scaling -Correspondence problems	-Multiples and factors -Square and cube numbers -Multiply numbers up to 4 digits by a 1-digit number -Multiply numbers up to 4 digits by a 2-digit number -Multiply by 10, 100 and 1,000 -Multiply by 10, 100 and 1,000 -Mental strategies -Multiply fractions by a whole number -Multiply mixed numbers by a whole number -Find the whole	-Multiply numbers up to 4 digits by a 2-digit number -Multiply by 10, 100 and 1,000 -Order of operations -Multiply decimals by integers -Multiply fractions by fractions -Find the whole -Calculations involving ratio

Progression of skills – Division

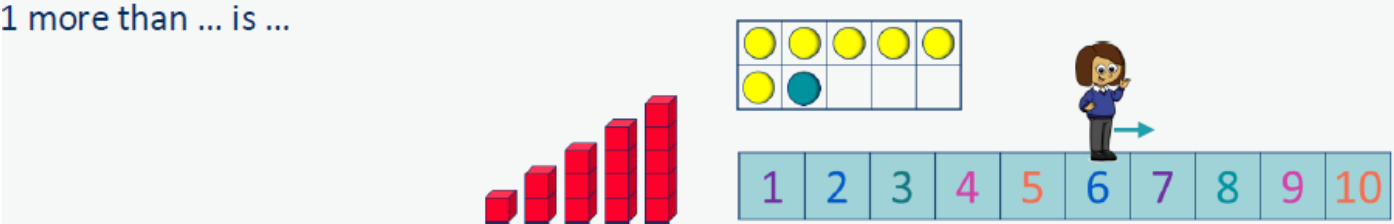
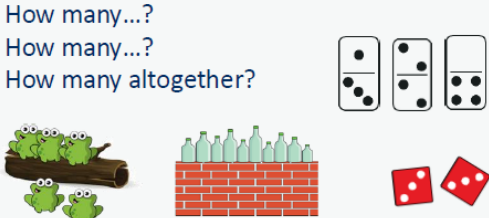
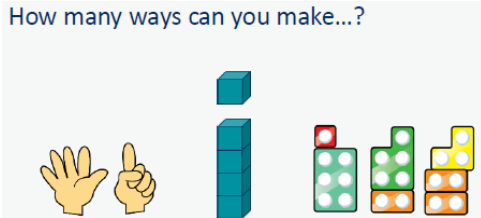
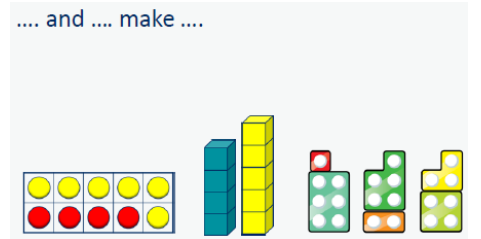
Nursery	Reception	Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
-Continue with counting and subitising skills as a foundation for later work on equal groups. (see addition and subtraction sections)	-Sharing -Grouping	-Make equal groups – grouping -Make equal groups – sharing -Find a half -Find a quarter	-Divide by 2 -Divide by 10 -Divide by 5 -Missing numbers -Unit fractions -Non-unit fractions	-Divide by 3 -Divide by 4 -Divide by 8 -Related facts -Divide a 2-digit number by a 1-digit number - no exchange -Divide a 2-digit number by a 1-digit number - with remainders -Unit fractions of a set of objects -Non-unit fractions of a set of objects	-Division facts to 12×12 -Divide a number by 1 and itself -Related facts -Divide a 2 or 3-digit number by a 1-digit number -Divide by 10 and 100	-Mental strategies -Divide numbers up to 4 digits by a 1-digit number -Divide by 10, 100 and 1,000 -Fraction of an amount	-Short division -Mental strategies -Long division -Order of operations -Divide by 10, 100 and 1,000 -Divide decimals by integers -Decimal and fraction equivalents -Divide a fraction by an integer -Fraction of an amount -Calculate percentages -Calculations involving ratio

RECEPTION

Reception Addition

Key Vocabulary:

1 more, add, add more, altogether, first, then, now, part, whole

Progression of Skills	Key Representations	
Conceptually subitise to 5 Notice the parts that make up the whole.	What do you see? How do you see it? 	
1 more Continue to link to stories, songs and rhymes.	1 more than ... is ... 	
Notice the composition of numbers within 10 Link to stories, songs and rhymes.	How many...? How many...? How many altogether? 	How many ways can you make...? 
Combine 2 groups 2 groups are combined to find the total.	There are There are There are altogether. 	 and make 

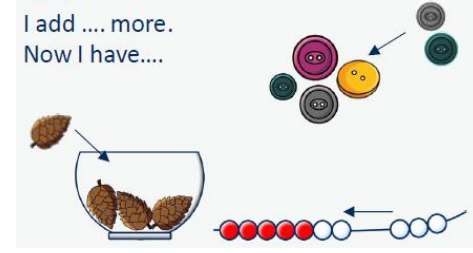
Add more

A quantity is increased.

First... Then.... Now....



I have
I add more.
Now I have....



Reception Subtraction

Key Vocabulary:

1 less, first, left, now, part, take away, whole

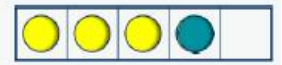
Progression of Skills

Key Representations

Conceptually subitise to 5

Notice the parts that make up the whole.

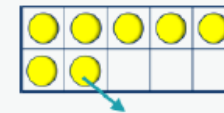
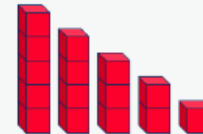
What do you see?
How do you see it?



1 less

Continue to link to stories, songs and rhymes.

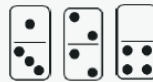
1 less than ... is ...



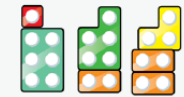
Notice the composition of numbers within 10

Link to stories, songs and rhymes.

How many...?
How many...?
How many altogether?



How many ways can you make...?



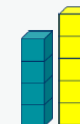
Partition

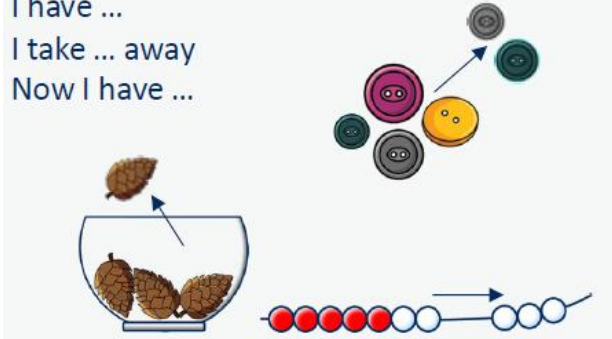
Using objects, explore different ways to partition a number into 2 or more parts.

There are ... altogether.
I can see ... here and ... there.



.... and make

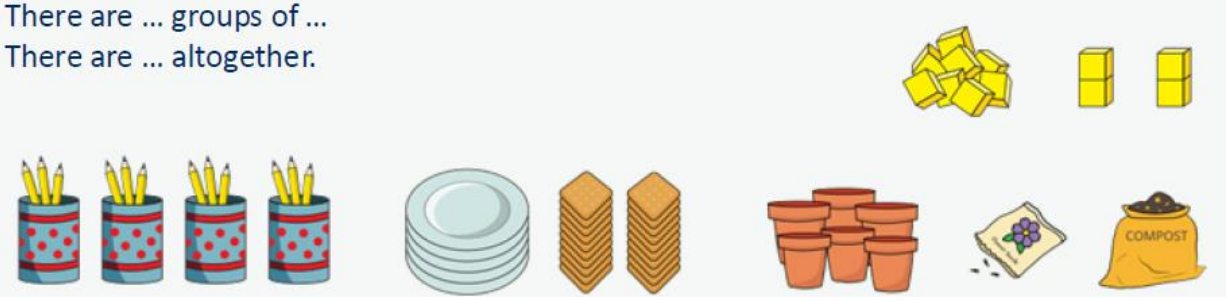


Take away A quantity is reduced.	First... Then... Now... 	I have ... I take ... away Now I have ... 
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Reception Multiplication

Key Vocabulary:

double, equal groups, even, fair, grouping, groups, odd, pair, sharing, unequal, groups

Progression of Skills	Key Representations
Double to 10 Prompt children to notice that double means twice as many and to notice that there are two equal groups.	Double ... is is double ... 
Make equal groups Provide opportunities to make equal groups when tidying up or during snack time. Encourage children to check that each group has the same amount.	There are ... groups of ... There are ... altogether. 

Reception Division

Key Vocabulary:

double, equal groups, even, fair, grouping, groups, odd, pair, sharing, unequal, groups

Progression of Skills

Key Representations

Sharing

Provide practical activities such as sharing items during snack time. Encourage children to check whether items have been shared fairly (equally).

There are ... altogether.

They are shared equally between ... groups.



Grouping

Provide opportunities to make equal groups when tidying up or during snack time. Encourage children to check that each group has the same amount.

There are ... groups of ...

There are ... altogether.

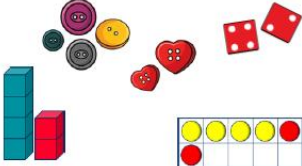
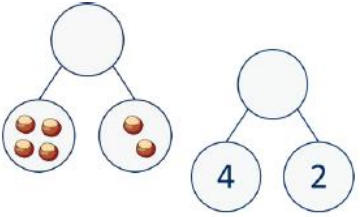
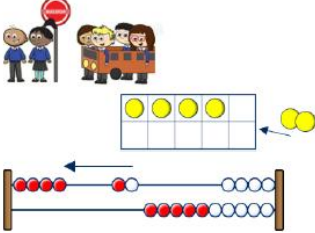
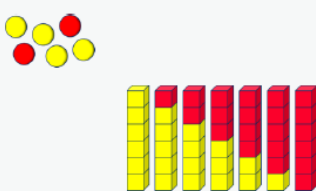
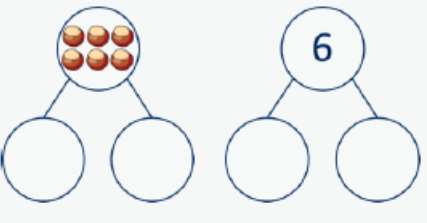


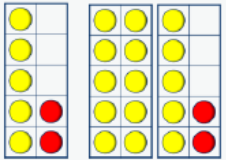
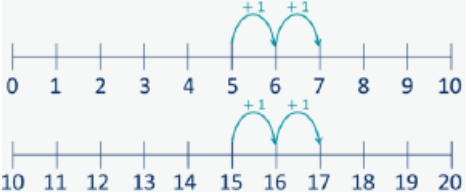
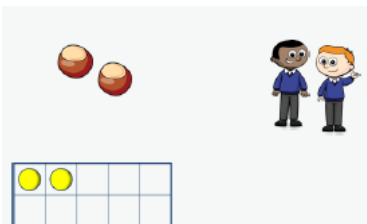
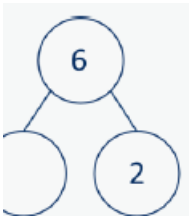
YEAR 1

Year 1 Addition

Key Vocabulary:

addition, add together, double, efficient, equal to, fact family, greater, group, inverse, near double, number bond, plus, symbol, systematic, total

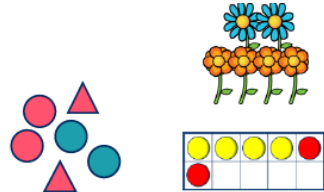
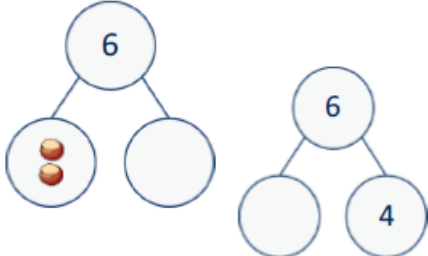
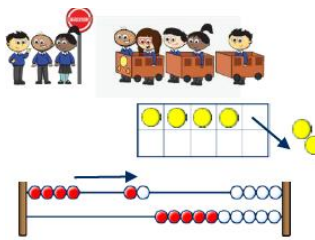
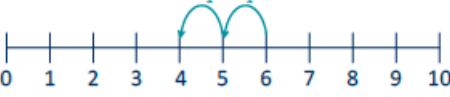
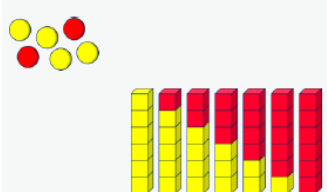
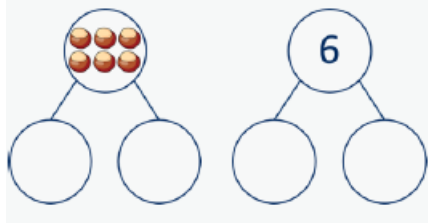
Progression of Skills	Concrete	Pictorial	Abstract
Add together (aggregation) 2 quantities are combined to find the total.	Objects, cubes, counters, base 10, tens frame etc There are ... There are ... There are ... altogether 	... is a part ... is a part ... is the whole. 	... plus ... is equal to... ... is equal to ... + ... $4 + 2 = 6$ $2 + 4 = 6$ $6 = 4 + 2$ $6 = 2 + 4$
Add more (augmentation) A quantity is increased.	Objects, cubes, counters, base 10, tens frame, rekenreks etc First... Then... Now... 	Number tracks/Number lines I start at... I jump on... I land on... 	... plus ... is equal to... ... is equal to ... + ... $4 + 2 = 6$ $2 + 4 = 6$ $6 = 4 + 2$ $6 = 2 + 4$ Start at 4 and count on 2.
Bonds within 10 Include bonds for each number within 10. Encourage children to notice patterns.	Base 10, counters, cubes, tens frame ... is made of ... and and ... make ... 	... can be partitioned into ... and ... 	... plus ... is equal to... $6 + 0 = 6$ $5 + 1 = 6$ $4 + 2 = 6$ $3 + 3 = 6$ $2 + 4 = 6$ $1 + 5 = 6$ $0 + 6 = 6$

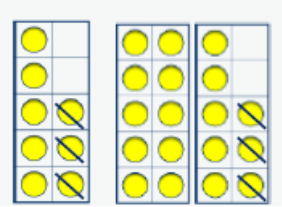
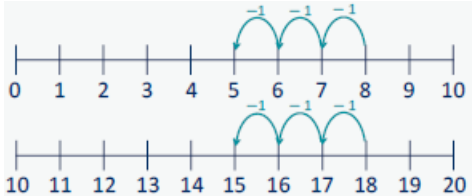
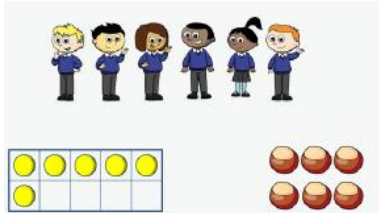
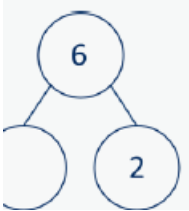
Related facts within 20 Make links to known facts.	Tens frame or Base 10 I know that ... and ... = ... so ... and ... = ... 	Use representations of tens frames or base 10 or numberlines ... more than ... is ... so ... more than ... is ... 	What patterns do you notice? $5 + 2 = 7$ $15 + 2 = 17$ $7 = 5 + 2$ $17 = 15 + 2$
Missing numbers Make links to known facts.	Objects, cubes, counters, base 10, tens frame etc How many more do you need to make ...? 	If ... is the whole and ... is a part, the other part must be ... 	... plus ... is equal to... $2 + \underline{\quad} = 6$ $6 = 2 + \underline{\quad}$

Year 1 Subtraction

Key Vocabulary:

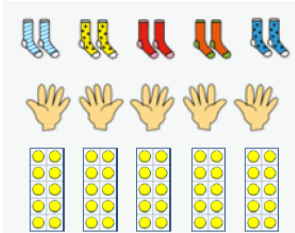
subtraction, subtract, difference, efficient, equal to, fact family, group, inverse, less, minus, near double, number bond, symbol, systematic

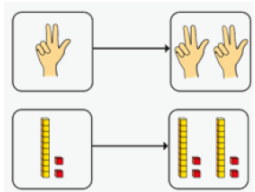
Progression of Skills	Concrete	Pictorial	Abstract
Find a part Link to number bonds and known facts	Objects, cubes, counters, base 10, tens frame etc There are ... in total ... are ... How many are not ...? 	... is the whole. ... is a part ... is a part 	... subtract ... is equal to... ... is equal to ... - ... $6 - 2 = 4$ $6 - 4 = 2$ $4 = 6 - 2$ $2 = 6 - 4$
Take away	Objects, cubes, counters, base 10, tens frame, rekenreks etc First... Then... Now... 	Number tracks/Number lines I start at... I jump back... I land on... 	... minus ... is equal to... ... is equal to ... - ... $6 - 2 = 4$ $6 - 4 = 2$ $4 = 6 - 2$ $2 = 6 - 4$
Bonds within 10 Focus on subtraction facts. Encourage children to notice patterns.	Base 10, counters, cubes, tens frame ... is made of ... and and ... make ... 	... can be partitioned into ... and ... 	... minus ... is equal to... $6 - 0 = 6$ $6 - 1 = 5$ $6 - 2 = 4$ $6 - 3 = 3$ $6 - 4 = 2$ $6 - 5 = 1$ $6 - 6 = 0$

Related facts within 10 Make links to know facts.	Tens frame or Base 10 I know that ... minus ... = ... so ... minus ... = ... 	Use representations of tens frames or base 10 or numberlines ... less than ... is ... so ... less than ... is ... 	What patterns do you notice? $8 - 3 = 5$ $18 - 3 = 15$ $5 = 8 - 3$ $15 = 18 - 3$
Missing numbers Make links to know facts.	Objects, cubes, counters, base 10, tens frame etc How many more do you need to subtract to make ...? 	If ... is the whole and ... is a part, the other part must be ... 	... minus ... is equal to... $6 - \underline{\quad} = 2$ $2 = 6 - \underline{\quad}$

Year 1 Multiplication

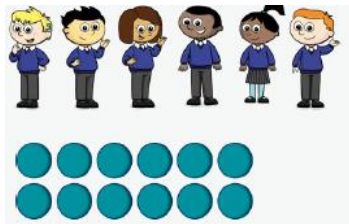
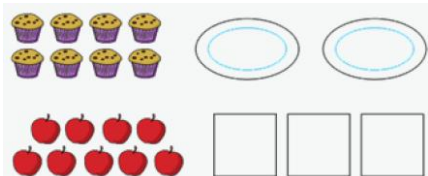
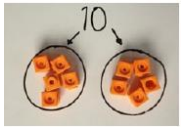
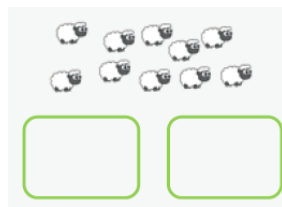
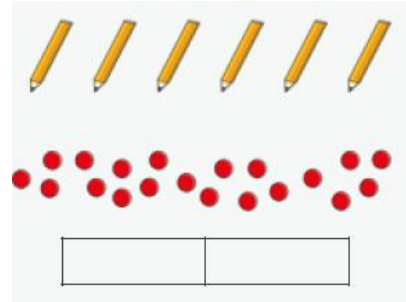
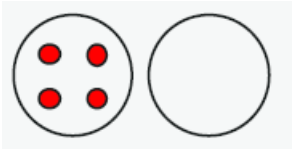
Key Vocabulary:
array, divide, repeated, addition

Progression of Skills	Concrete	Pictorial	Abstract
Count in 2s, 5s and 10s	Counters/cubes/equipment. Make groups of 2, 5 and 10 and count in 2s, 5s and 10s There are ... equal groups of ... There are ... altogether 	Count in 2s, 5s, 10s using pictures, drawings of repeated groups, hundred square, numberlines, numbertracks 	Count groups on fingers
Add equal groups (repeated addition)	Base 10/cubes/counters/equipment There are ... equal groups of ... There are ... altogether. 	Count equal groups using pictures or drawings of repeated groups 	$2 + 2 + 2 = 6$
Make arrays	Counters/cubes/equipment There are ... rows of ... There are ... altogether. There are ... columns of ... There are ... altogether. 	Draw arrays and circle groups 	2 and 2 and 2 and 2 and 2 equals 10

Make doubles	Base 10/cubes/counters/equipment Double ... is + ... = ...  The illustrations show two methods of doubling. The top method uses hands: one hand with two fingers up is shown, followed by an arrow pointing to two hands each with two fingers up. The bottom method uses base 10 blocks: one rod (10 units) and two units are shown, followed by an arrow pointing to two rods and four units.	Draw two equal groups of Base 10/cubes/counters/equipment  The illustration shows two groups of four red cubes each, separated by a blue arrow pointing from the first group to the second.	$4 + 4 = 8$
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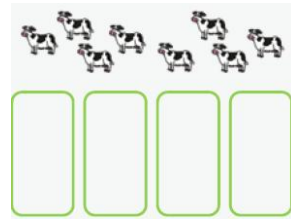
Year 1 Division

Key Vocabulary:
array, divide, repeated, addition

Progression of Skills	Concrete	Pictorial	Abstract
Make equal groups – grouping	Counters/cubes/equipment/objects. There are ... altogether. How many groups of ... can you make? 	Draw representations of Counters/cubes/equipment. There are ... groups of ... 	2, 4, 6, 8, 10, 12 – 6 equal groups of 2
Make equal groups – sharing	Base 10/cubes/counters/equipment/objects ... have been shared equally between... There are ... on/in each ... 	Draw representations of Counters/cubes/equipment. 	2, 4, 6, 8, 10, 12 – 6 equal groups of 2 12 shared between ... is ...
Find a half	To find half, I need to share into 2 equal groups.  There are ... in each group.	Half of ... is ... 	If ... is half, what is the whole?  4 is half of ...

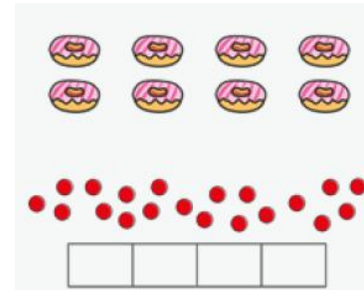
Find a quarter

To find a quarter, I need to share into 4 equal groups.

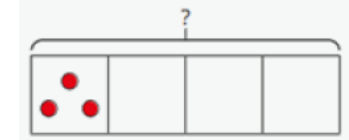


There are ... in each group.

A quarter of ... is ...



If ... is one quarter, what is the whole?



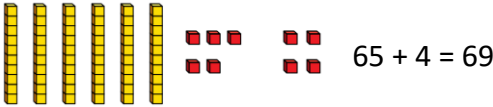
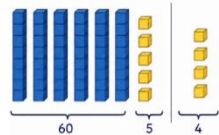
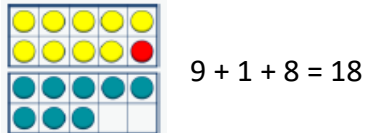
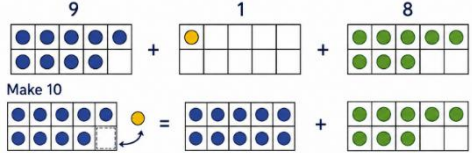
3 is one quarter of ...

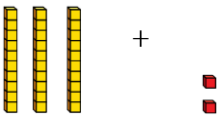
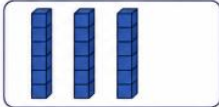
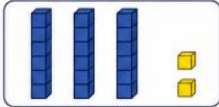
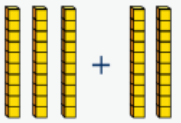
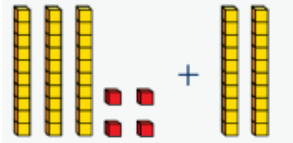
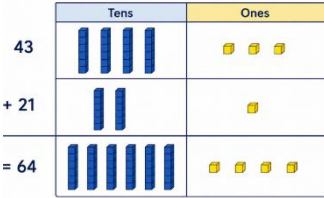
YEAR 2

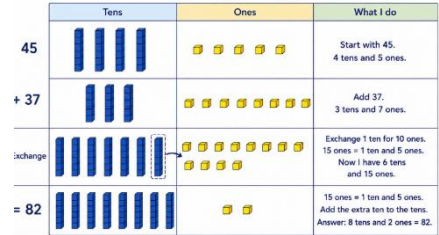
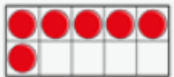
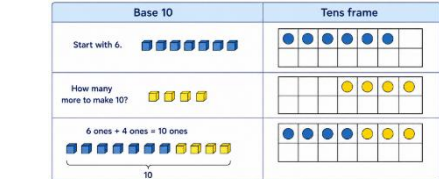
Year 2 Addition

Key Vocabulary:

calculation, exchange, method, multiple, one(s), operation, partition, related facts, ten(s), value, increase, sum

Progression of Skills	Concrete	Pictorial	Abstract
Add ones to any number	... plus ... is equal to... ... is equal to ... + ... Base 10  $65 + 4 = 69$	... plus ... is equal to... ... is equal to ... + ... Use representations of base 10 and tens frame. 	... plus ... is equal to... ... is equal to ... + ... $65 + 4 = 69$ Recall of number facts must be secure by this point $5 + 4 = 9$
Add three 1-digit numbers	Tens frame or Base 10 Combine to make 10 or bridge 10, then add the third digit ... and ... are a bond to 10  $9 + 1 + 8 = 18$	Draw representations – look for bonds to ten or make 10 	What do you notice? Which addition is the easiest to calculate? $8 + 9 + 1 =$ $8 + 1 + 9 =$ $9 + 1 + 8 =$
Add across a ten	Base 10 or Tens frame $25 + 7 = 32$  Partition the number being added to make a full ten (exchange) ... can be partitioned into ... and ...	Use representations of base 10 and tens frame.	I add ... to get to ... then I add ... $25 + 7 = 32$ $25 + 5 = 30$ $30 + 2 = 32$

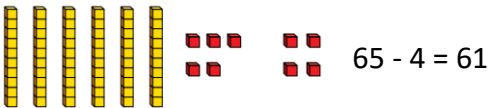
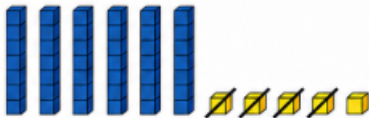
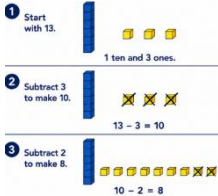
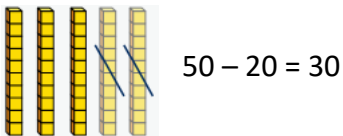
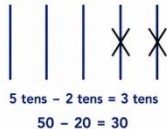
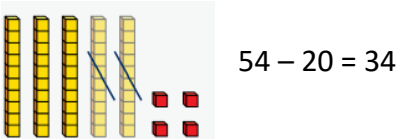
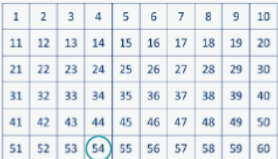
	 $30 + 2 = 32$	$25 + 5 = 30$  $30 + 2 = 32$ 	
Add multiples of 10	Base 10 ... tens + ... tens = ... tens  $30 + 20 = 50$	Use representations of base 10. Draw tens and ones. 	$30 + 20 = 50$ $20 + 30 = 50$ $50 = 30 + 20$ $50 = 20 + 30$
Add 10s to any number	Base 10 ... tens + ... tens = ... tens ... tens and ... ones =  $34 + 20 = 54$	Base 10 or 100 square To add ... I need to add 10 ... times 	$34 + 20 = 54$ $34 + 10 = 44$ $44 + 10 = 54$
Add 2-digit numbers (not crossing a ten)	Base 10. Lining up ones and tens in columns will support with later written methods. ... ones + ... ones = ... ones ... tens + ... tens = ... tens  $43 + 21 = 64$	Use representations of base 10. Draw tens and ones. 	Partitioning tens and ones $3 \text{ ones} + 1 \text{ one} = 4 \text{ ones}$ $4 \text{ tens} + 2 \text{ tens} = 6 \text{ tens}$ $6 \text{ tens} + 4 \text{ ones} = 64$ $40 + 20 = 60$ $3 + 1 = 4$ $60 + 4 = 64$

Add 2-digit numbers (crossing a ten) Begin to exchange 10 ones for a ten	Base 10. Exchange 10 ones for 1 ten. There are ... ones so I do/do not need to make an exchange. $45 + 37 = 82$ 	Use representations of base 10. Draw tens and ones. 	Partitioning tens and ones 5 ones + 7 ones = 12 ones 12 ones = 1 ten and 2 ones 4 tens + 3 tens + 1 ten = 8 tens 8 tens + 2 ones = 82 $40 + 30 = 70$ $5 + 7 = 12$ $70 + 12 = 82$
Missing numbers	Tens frame or Base 10. How many more do you need to make ...?  $6 + \underline{\quad} = 10$	Use representations of base 10 and tens frame. 	$6 + 4 = 10$ $4 + 6 = 10$ $10 = 6 + 4$ $10 = 4 + 6$

Year 2 Subtraction

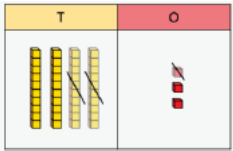
Key Vocabulary:

calculation, exchange, method, multiple, one(s), operation, partition, related facts, ten(s), value, decrease, sum

Progression of Skills	Concrete	Pictorial	Abstract
Subtract ones from any number	Base 10 ... subtract ... is equal to is equal to ... - ... 	Use representations of base 10 and tens frame. ... subtract ... is equal to is equal to ... - ... 	... subtract ... is equal to is equal to ... - ... $65 - 4 = 61$ Recall of number facts must be secure by this point $5 - 4 = 1$
Subtract across a ten	 $13 - 5 = 8$ Partition the number being taken away, e.g. 5 is made of 3 and 2. ... can be partitioned into ... and ...	Use representations of base 10 and tens frame. 	$13 - 5 = 8$ $5 = 3 + 2$ $5 = 2 + 3$
Subtract multiples of 10	Base 10 ... tens - ... tens = ... tens 	Use representations of base 10. Draw tens and ones 	$50 - 20 = 30$ $50 - 30 = 20$ $30 + 20 = 50$ $20 + 30 = 50$
Subtract 10s from any number	Base 10 ... tens - ... tens = ... tens ... tens and ... ones = ... 	Base 10 or 100 square To subtract ... I need to subtract 10 ... times. 	$54 - 20 = 34$ $54 - 10 = 44$ $44 - 10 = 34$

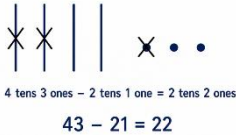
Subtract two 2-digit numbers (not across a ten)

Base 10
 ... ones - ... ones = ... ones
 ... tens - ... tens = ... tens



$$43 - 21 = 22$$

Use representations of base 10.
 Draw tens and ones.

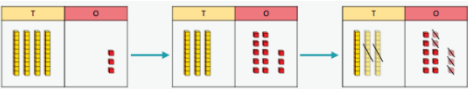


$$43 - 21 = 22$$

Partitioning tens and ones

3 ones - 1 one = 2 ones ($3 - 1 = 2$)
 4 tens - 2 tens = 2 tens ($40 - 20 = 20$)
 2 tens and 2 ones = 22 ($20 + 2 = 22$)

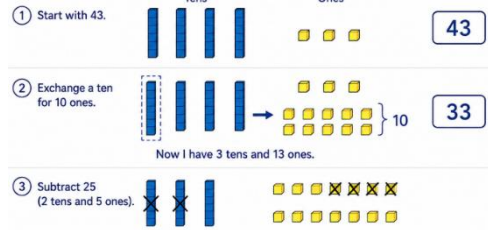
Subtract two 2-digit numbers (across a ten)



$$43 - 25 = 18$$

Begin to exchange 1 ten for 10 ones.
 I need to make an exchange because
 I do not have enough ones to
 subtract ... ones.

Use representations of base 10.
 Draw tens and ones.

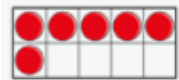


Partitioning tens and ones

3 ones - 5 ones (I need to exchange
 1 ten for 10 ones)
 13 ones - 5 ones = 8 ones
 3 tens - 2 tens = 1 ten
 1 ten and 8 ones = 18

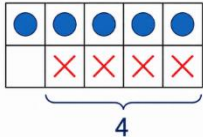
Missing numbers

Tens frame or Base 10.
 How many do you need to subtract
 to make ...?



$$10 - \underline{\quad} = 6$$

Use representations of base 10 and
 tens frame.

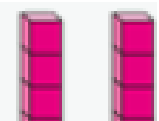
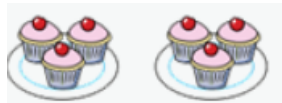
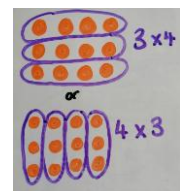
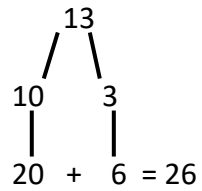


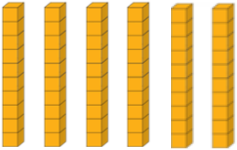
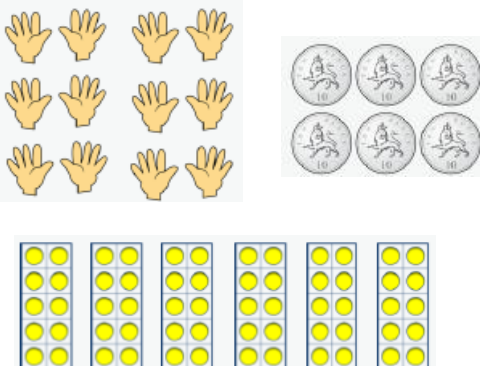
$10 - 4 = 6$
 $10 - 6 = 4$
 $6 = 10 - 4$
 $4 = 10 - 6$

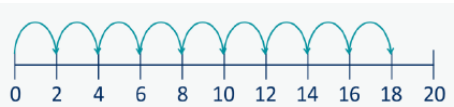
Year 2 Multiplication

Key Vocabulary:

even, lots of, multiply, odd, twice, times, times-table

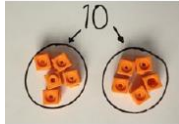
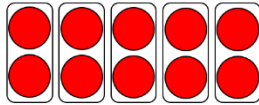
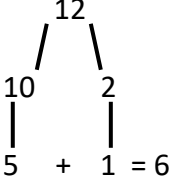
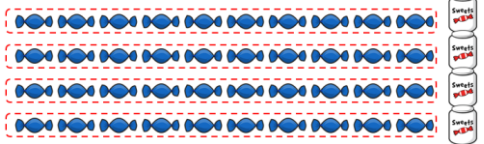
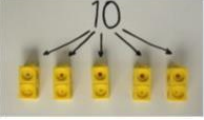
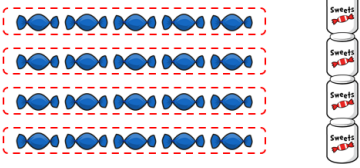
Progression of Skills	Concrete	Pictorial	Abstract
Link repeated addition and multiplication	Base 10/cubes/counters/equipment There are ... equal groups with ... in each group. There are ... altogether.  $3 + 3 = 6$ $2 \times 3 = 6$	Count equal groups using pictures or drawings of repeated groups 	$3 + 3 = 6$ $2 \times 3 = 6$
Use arrays	Counters/cubes/equipment There are ... rows with ... in each row. There are ... columns with ... in each column.  2×5 or 5×2 3×4 or 4×3	Draw arrays and circle groups in 2 ways to show Commutativity 	Instant recall or using arrays to write the equation I can see ... x ... and ... x ... $3 \times 4 = 12$ $4 \times 3 = 12$ $3 \times 4 = 4 \times 3$
Double	Base 10/cubes/counters/equipment  Double ... is ... Double 4 = 4 + 4 Double 4 is 8  Double 2 = 2 + 2 Double 2 is 4	Draw the same number again 	Partition mentally  $20 + 6 = 26$

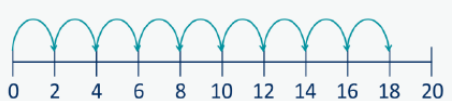
The 2-times table	Counters/cubes/equipment. Make groups of 2 and count in 2s  4 lots of 2 = 8 $4 \times 2 = 8$	Count in 2s using pictures or drawings of repeated groups 	Count groups on fingers ... times 2 is equal to ... Instant recall of 2-times table facts, e.g. $4 \times 2 = 8$ or 4 lots of 2 = 8
The 10-times table	Counters/cubes/equipment. Make groups of 10 and count in 10s  6 lots of 10 = 60 $6 \times 10 = 60$	Count in 10s using pictures or drawings of repeated groups 	Count groups on fingers ... times 10 is equal to ... Instant recall of 10-times table facts, e.g. $6 \times 10 = 60$ or 6 lots of 10 = 60
The 5-times table	Counters/cubes/equipment. Make groups of 5 and count in 5s  5 lots of 5 = 25 $5 \times 5 = 25$	Count in 5s using pictures or drawings of repeated groups 	Count groups on fingers ... times 5 is equal to ... Instant recall of 5-times table facts, e.g. $5 \times 5 = 25$ or 5 lots of 5 = 25

Missing numbers	Objects, counters, cubes, base 10 etc ... is equal to ... groups of ... 18 socks, how many pairs? 	Count in 2s, 5s and 10s using numberlines, pictures or drawings of repeated groups 	... times ... is equal to ... ___ x 2 = 18 18 = 2 x ___
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Year 2 Division

Key Vocabulary:
divide, even, half, odd, twice, times, times-table

Progression of Skills	Concrete	Pictorial	Abstract
Divide by 2	Counters/cubes/equipment. Share equipment equally between groups.  10 shared equally between 2 is 5 $10 \div 2 = 5$	Use pictures to share amounts.  There are 5 equal groups of 2 $10 \div 2 = 5$	Know half of a number by partitioning in head.  12 $\swarrow \quad \searrow$ $10 \quad 2$ $\mid \quad \mid$ $5 \quad + \quad 1 = 6$
Divide by 10	Counters/cubes/equipment. Share equipment equally between groups.  30 shared equally between 10 is 3 $30 \div 10 = 3$	Use pictures to share amounts.  There are 4 equal groups of 10 $40 \div 10 = 4$	$40 \div 10 = 4$ 4 tens $\div 10 = 4$
Divide by 5	Counters/cubes/equipment. Share equipment equally between groups.  10 shared equally between 5 is 2 $10 \div 5 = 2$	Use pictures to share amounts.  There are 4 equal groups of 5 $20 \div 5 = 4$	$20 \div 5 = 4$

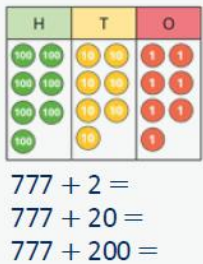
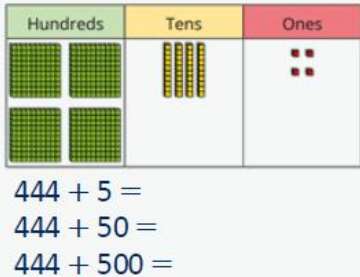
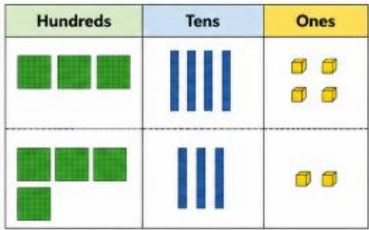
Missing numbers	Objects, counters, cubes, base 10 etc ... divided by 2/5/10 is equal to ... 18 socks, how many pairs? 18 divided by 2 is equal to ... 	Count in 2s, 5s and 10s using numberlines, pictures or drawings of repeated groups 	... divided by 2/5/10 is equal to ... $18 \div 2 = 9$
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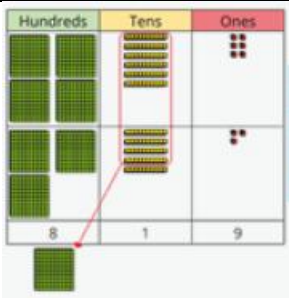
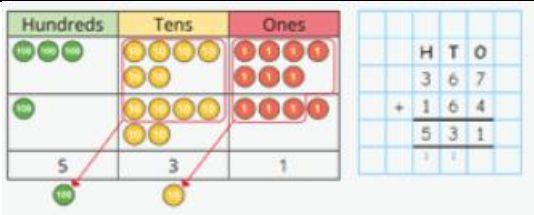
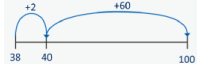
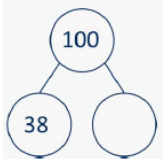
YEAR 3

Year 3 Addition

Key Vocabulary:

column, addition, digit, estimate, exchange, hundred(s), inverse, crossing the 10, crossing the 100

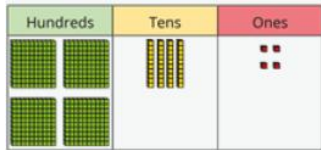
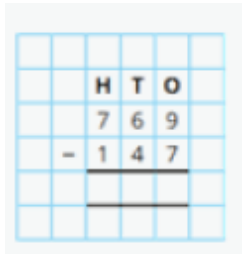
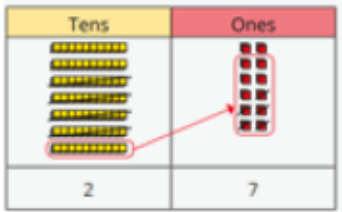
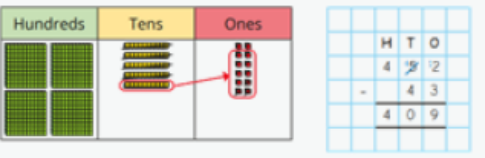
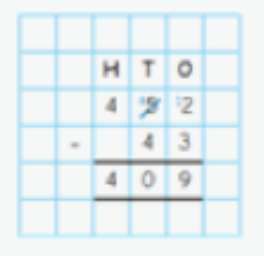
Progression of Skills	Concrete	Pictorial	Abstract
Add 1s, 10s or 100s to a 3-digit number	Base 10, place value chart 	Draw representations of Base 10 	What patterns do you notice? $235 + 3 =$ $235 + 30 =$ $235 + 300 =$ $604 + 20 =$ $604 + 50 =$ $604 + 90 =$
Add two numbers (no exchange)	Base 10/place-value counters ... ones + ... ones = ... ones ... tens + ... tens = ... tens ... hundreds + ... hundreds = ... hundreds 	Introduction of formal method – column addition (using representations, such as place value grid/counters, to support) 	Column addition $345 + 432 =$ 
Add two numbers across a 10 or 100 Formal written method involving up to 2 exchanges including 3-digit plus 2-digit numbers.	Base 10/place-value counters There are ... ones, so I do/do not need to make an exchange. There are ... tens, so I do/do not need to make an exchange. ... ones = ... ten and ... ones. ... tens = ... hundred and ... tens.	Formal method – column addition (using representations, such as place value grid/counters, to support)	Column addition $367 + 164 =$ 

			
Complements to 100	Base 10 ... plus ... is equal to 100 $62 + 38 = 100$ 	Part whole models, bar models, numberlines, hundred squares I add ... to get to the next 10, then ... to get to 100  $38 + 62 = 100$ $62 + 38 = 100$ $100 = 38 + 62$ $100 = 62 + 38$ 	$38 + 62 = 100$ $62 + 38 = 100$ $100 = 38 + 62$ $100 = 62 + 38$

Year 3 Subtraction

Key Vocabulary:

column, subtraction, digit, estimate, exchange, hundred(s), inverse, crossing the 10, crossing the 100

Progression of Skills	Concrete	Pictorial	Abstract
Subtract 1s, 10s or 100s from a 3-digit number	Base 10, place value chart  $777 - 4 =$ $777 - 40 =$ $777 - 400 =$	Draw representations of Base 10  $444 - 2 =$ $444 - 20 =$ $444 - 200 =$	What patterns do you notice? $235 - 3 =$ $235 - 30 =$ $235 - 300 =$ $624 - 20 =$ $654 - 50 =$ $694 - 90 =$
Subtract two numbers (no exchange)	Base 10/place-value counters ... ones - ... ones = ... ones ... tens - ... tens = ... tens ... hundreds - ... hundreds = ... hundreds 	Introduction of formal method – column subtraction (using representations, such as place value grid/counters, to support) 	Column subtraction $769 - 147 =$ 
Add two numbers across a 10 or 100 Formal written method involving up to 2 exchanges including 3-digit subtract 2-digit numbers.	Base 10/place-value counters I need to subtract ... ones. I do/do not need to make an exchange. I need to subtract ... tens. I do/do not need to make an exchange. I can exchange 1 ... for 10 ... 	Formal method – column subtraction (using representations, such as place value grid/counters, to support) 	Column subtraction $452 - 43 = 409$ 

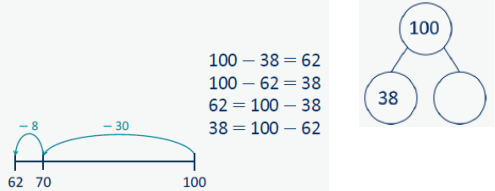
Complements to 100

Base 10
... minus ... is equal to ...

	100 - 62 = 38	
	Tens	Ones
1. Start with 100 (10 tens, 0 ones)		
2. Exchange 1 ten for 10 ones		
3. Remove 62 (6 tens and 2 ones)		
4. 38 remains		

Part whole models, bar models, numberlines, hundred squares

I subtract ... tens, then I subtract ... ones.

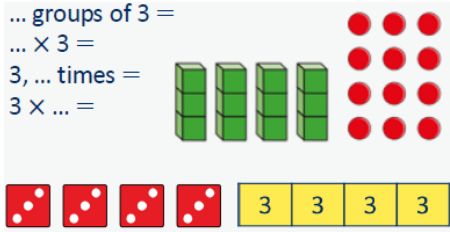
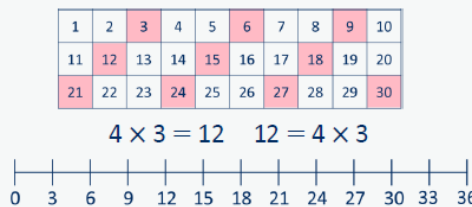
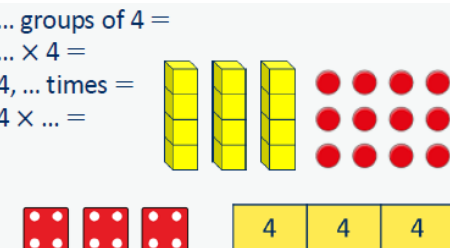
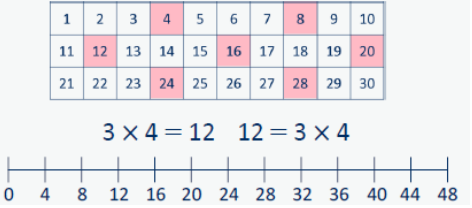
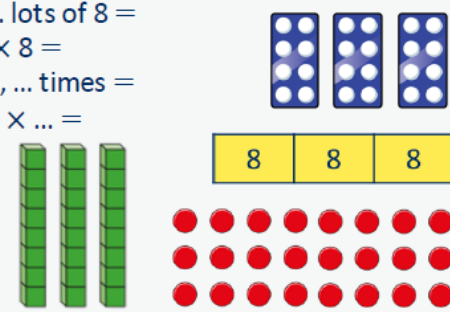
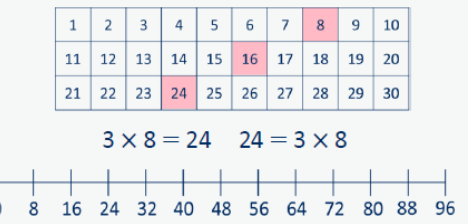


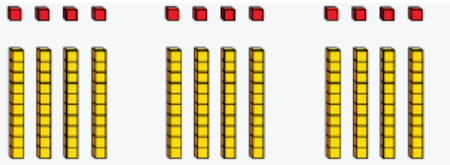
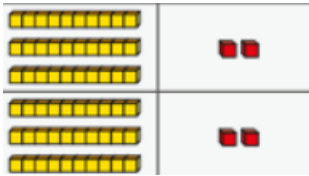
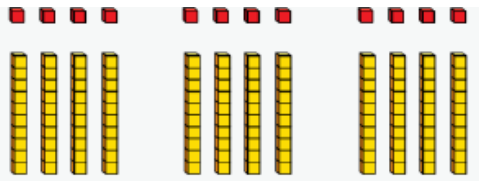
$100 - 38 = 62$
 $100 - 62 = 38$
 $62 = 100 - 38$
 $38 = 100 - 62$

Year 3 Multiplication

Key Vocabulary:

commutative, inverse, multiple, product, remainder, scaling

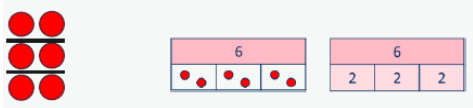
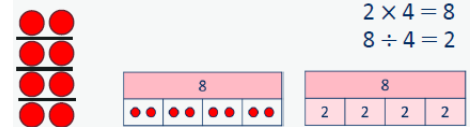
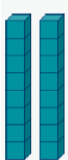
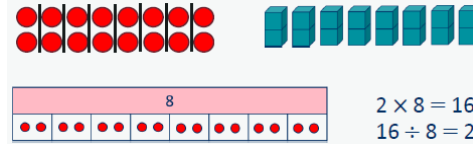
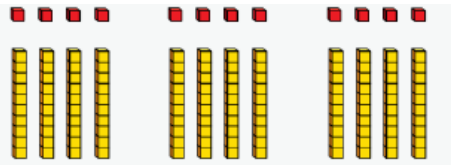
Progression of Skills	Concrete	Pictorial	Abstract
The 3 times-table	Cubes, counters, dice, equipment ... groups of 3 = ... $\times 3$ = 3, ... times = $3 \times \dots$ = 	Numberline, numbertrack, hundred square, drawings ... times 3 is equal to ...  $4 \times 3 = 12$ $12 = 4 \times 3$	$4 \times 3 = 12$ $12 = 4 \times 3$
The 4 times-table	Cubes, counters, dice, equipment ... groups of 4 = ... $\times 4$ = 4, ... times = $4 \times \dots$ = 	Numberline, numbertrack, hundred square, drawings ... times 4 is equal to ...  $3 \times 4 = 12$ $12 = 3 \times 4$	$3 \times 4 = 12$ $12 = 3 \times 4$
The 8 times-table	Cubes, counters, dice, equipment ... lots of 8 = $\times 8$ = 8, ... times = $8 \times \dots$ = 	Numberline, numbertrack, hundred square, drawings ... times 8 is equal to ...  $3 \times 8 = 24$ $24 = 3 \times 8$	$3 \times 8 = 24$ $24 = 3 \times 8$

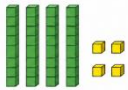
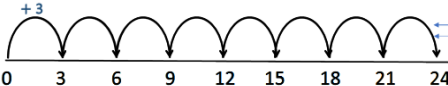
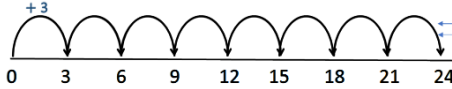
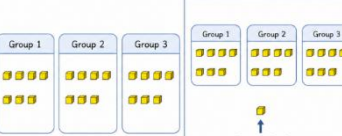
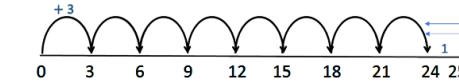
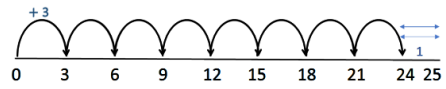
Related facts Use knowledge of multiplying by 10 to scale times-table facts	Base 10, place value counters ... × ... ones is equal to ... ones So ... x ... tens is equal to ... tens 	Use/draw representations of base 10/place value counters 	3 x 4 = 12 3 x 40 = 120										
Multiply a 2-digit number by a 1-digit number – no exchange	Base 10 or place-value counters arranged into equal groups 32 x 2 = 	Introduction of formal method – short multiplication (using representations, such as place value grid/counters, to support) <table border="1" data-bbox="1131 577 1388 745"><thead><tr><th>Tens</th><th>Ones</th></tr></thead><tbody><tr><td>10 10</td><td>1</td></tr><tr><td>10 10</td><td>1</td></tr><tr><td>10 10</td><td>1</td></tr><tr><td>10 10</td><td>1</td></tr></tbody></table> $\begin{array}{r} 21 \\ \times 4 \\ \hline 84 \end{array}$	Tens	Ones	10 10	1	10 10	1	10 10	1	10 10	1	Short multiplication 21 x 4 = 84 $\begin{array}{r} 21 \\ \times 4 \\ \hline 84 \end{array}$
Tens	Ones												
10 10	1												
10 10	1												
10 10	1												
10 10	1												
Multiply a 2-digit number by a 1-digit number – with exchange	Base 10 or place-value counters arranged into equal groups or make arrays using manipulatives 44 x 3 = 	Formal method – short multiplication (using representations, such as place value grid/counters, to support) <table border="1" data-bbox="1131 952 1426 1099"><thead><tr><th>Tens</th><th>Ones</th></tr></thead><tbody><tr><td>10 10 10</td><td>1 1 1 1 1</td></tr><tr><td>10 10 10</td><td>1 1 1 1 1</td></tr><tr><td>10 10 10</td><td>1 1 1 1 1</td></tr></tbody></table> $\begin{array}{r} 45 \\ \times 3 \\ \hline 135 \end{array}$	Tens	Ones	10 10 10	1 1 1 1 1	10 10 10	1 1 1 1 1	10 10 10	1 1 1 1 1	Short multiplication 45 x 3 = 135 $\begin{array}{r} 45 \\ \times 3 \\ \hline 135 \end{array}$		
Tens	Ones												
10 10 10	1 1 1 1 1												
10 10 10	1 1 1 1 1												
10 10 10	1 1 1 1 1												

Year 3 Division

Key Vocabulary:

commutative, inverse, multiple, product, remainder, scaling

Progression of Skills	Concrete	Pictorial	Abstract
Divide by 3	Cubes, counters, equipment There are ... groups of 3 in $\div 3 =$... 	Use representations/drawings of manipulatives, numberlines, bar models 	$2 \times 3 = 6$ $6 \div 3 = 2$
Divide by 4	Cubes, counters, equipment There are ... groups of 4 in $\div 4 =$... 	Use representations/drawings of manipulatives, numberlines, bar models 	$2 \times 4 = 8$ $8 \div 4 = 2$
Divide by 8	Cubes, counters, equipment There are ... groups of 8 in $\div 8 =$... $2 \times 8 = 16$ $16 \div 8 = 2$ 	Use representations/drawings of manipulatives, numberlines, bar models 	$2 \times 8 = 16$ $16 \div 8 = 2$
Related facts Link to known times-table facts	Base 10, place value counters ... $\div$... is equal to ..., So ... tens $\div$... is equal to ... tens. 	Use/draw representations of base 10/place value counters 	$12 \div 3 = 4$ $120 \div 3 = 40$

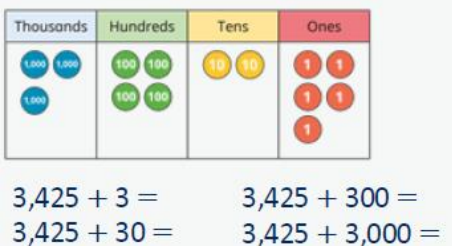
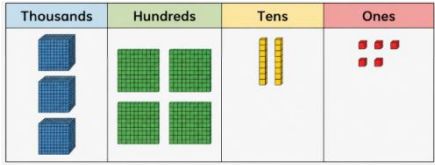
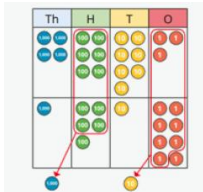
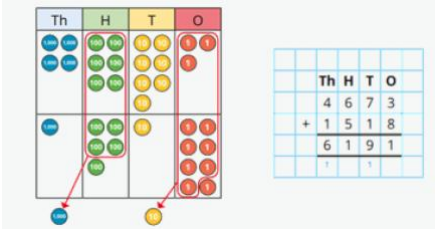
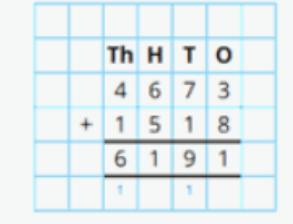
Divide a 2-digit number by a 1-digit number – no exchange	Base 10 or place-value counters arranged into equal groups ... tens divided by ... is equal to ... tens. ... ones divided by ... is equal to ... ones. <table><tr><th>Tens</th><th>Ones</th></tr><tr><td></td><td></td></tr><tr><td></td><td></td></tr><tr><td></td><td></td></tr><tr><td></td><td></td></tr></table> $60 \div 2 = 30$ $4 \div 2 = 2$ $64 \div 2 = 32$	Tens	Ones									Introduction of formal method – numberline (using representations, such as place value grid/counters, to support) 1. Make 24 using Base 10.  24 = 2 tens and 4 ones 2. Share equally into 3 groups. Group 1 Group 2 Group 3  Each group has 2 tens and 2 ones. (That's 8) 3. Count the groups. 3 groups of 8 = 24 $24 \div 3 = 8$  (Move to bus stop method when/if ready)	Numberline $24 \div 3 = 8$  (Move to bus stop method when/if ready)
Tens	Ones												
													
													
													
													
Divide a 2-digit number by a 1-digit number – with exchange	Base 10 or place-value counters arranged into equal groups ... tens divided by ... is equal to ... tens. ... ones divided by ... is equal to ... ones. <table><tr><th>Tens</th><th>Ones</th></tr><tr><td></td><td></td></tr><tr><td></td><td></td></tr><tr><td></td><td></td></tr><tr><td></td><td></td></tr></table> $80 \div 4 = 20$ $16 \div 4 = 4$ $96 \div 4 = 24$	Tens	Ones									Formal method – numberline (using representations, such as place value grid/counters, to support) 1. Make 25 using Base 10.  25 = 2 tens and 5 ones Exchange 1 ten for 10 ones.  Now we have 15 ones. 2. Share equally into 3 groups. Group 1 Group 2 Group 3  15 ones shared into 3 groups. Each group has 5 ones. (That's 15) Remainder 1 3. Count the groups and see what is left. 8 groups of 3 = 24 1 left over $25 \div 3 = 8 \text{ remainder } 1$  (Move to bus stop method when/if ready)	Numberline $25 \div 3 = 8r1$  (Move to bus stop method when/if ready)
Tens	Ones												
													
													
													
													

YEAR 4

Year 4 Addition

Key Vocabulary:

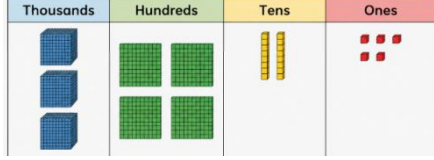
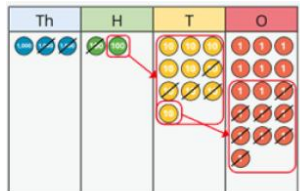
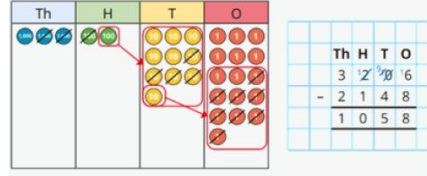
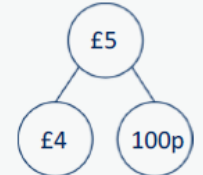
column, addition, digit, estimate, exchange, hundred(s), crossing the 10, crossing the 100, efficient, inverse, round, thousand(s)

Progression of Skills	Concrete	Pictorial	Abstract
Add 1s, 10s or 100s to a 4-digit number	Base 10, place value chart 	Draw representations of Base 10 	What patterns do you notice? $2350 + 3 =$ $2350 + 30 =$ $2350 + 300 =$ $2350 + 3000 =$ $6040 + 200 =$ $6040 + 500 =$ $6040 + 900 =$
Add up to two 4-digit numbers	Base 10/place-value counters There are ... ones/tens/hundreds so I do/do not need to make an exchange. I can exchange 10 ... for 1 ... 	Formal method – column addition (using representations, such as place value grid/counters, to support) 	Column addition $4673 + 1518 = 6191$ 
Add decimal numbers in the context of money	... pence + ... pence = ... pence ... pounds + ... pounds = ... pounds  $45p + 25p = 70p$ $£2 + £3 = £5$ $£5 + 70p = £5.70$		

Year 4 Subtraction

Key Vocabulary:

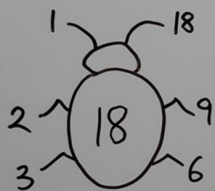
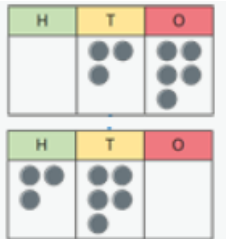
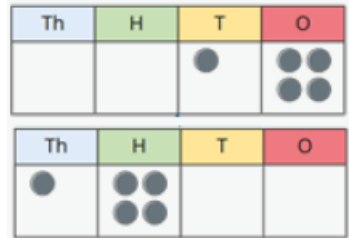
column, subtraction, digit, estimate, exchange, hundred(s), crossing the 10, crossing the 100, efficient, inverse, round, thousand(s)

Progression of Skills	Concrete	Pictorial	Abstract
Subtract 1s, 10s, 100s and 1000s from a 4-digit number	Base 10, place value chart  $3,425 - 2 =$ $3,425 - 200 =$ $3,425 - 20 =$ $3,425 - 2,000 =$	Draw representations of Base 10 	What patterns do you notice? $4356 - 3 =$ $4356 - 30 =$ $4356 - 300 =$ $4356 - 3000 =$ $6940 - 200 =$ $6940 - 300 =$ $6940 - 400 =$
Subtract up to two 4-digit numbers	Base 10/place-value counters I need to subtract... ones/tens/hundreds. I do/do not need to make an exchange. I can exchange 1... for 10... 	Formal method – column subtraction (using representations, such as place value grid/counters, to support) 	Column subtraction $3206 - 2148 = 1058$ 
Subtract decimal numbers in the context of money	I can partition £... into £... and 100p $£... - £... = £...$ $100p - ...p = ...p$ $£5 - £3.26$ $£4 - £3 = £1$ $100p - 26p = 74p$ $£5 - £3.26 = £1.74$ 		

Year 4 Multiplication

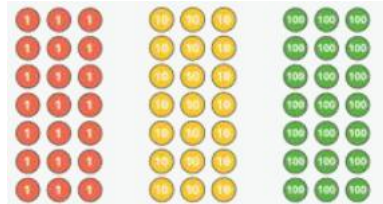
Key Vocabulary:

commutative, inverse, multiple, product, remainder, scaling, factor, factor pair, inverse, triple, efficient

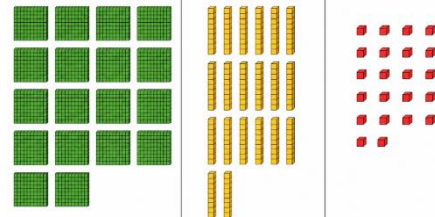
Progression of Skills	Concrete	Pictorial	Abstract
Multiply 3 numbers	Base 10, cubes, manipulatives To work out ... x ..., I can first calculate ... x ... and then multiply the answer by ...  $4 \times 2 \times 3 = 8 \times 3 = 24$ $2 \times 3 \times 4 = 6 \times 4 = 24$ $3 \times 4 \times 2 = 12 \times 2 = 24$	Use representations of cubes etc 	$4 \times 2 \times 3 = 8 \times 3 = 24$ $2 \times 3 \times 4 = 6 \times 4 = 24$ $3 \times 4 \times 2 = 12 \times 2 = 24$
Factor pairs	Factor Bugs  1×18 2×9 3×6		
Multiply by 10 and 100	Place value grid & counters When I multiply by 10/100, the digits move... place value column to the left. ... is 10/100 times the size of ... 	Use representations/drawings of place value grid & counters 	$35 \times 10 = 350$ $14 \times 100 = 1400$

Related facts

Base 10, place value counters
... × ... ones is equal to ... ones
So ... × ... tens is equal to ... tens
And ... × ... hundreds is equal to ... hundreds



Use/draw representations of base 10/place value counters

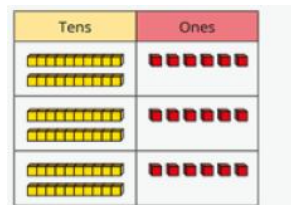


$$\begin{aligned} 3 \times 7 &= 21 \\ 3 \times 70 &= 210 \\ 3 \times 700 &= 2100 \end{aligned}$$

Mental strategies

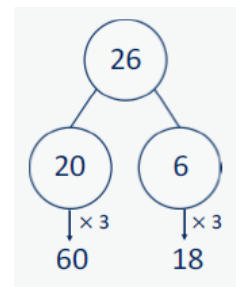
Partition 2 or 3-digit numbers to multiply using informal methods.

Base 10
... tens multiplied by ... is equal to ... tens.
... ones multiplied by ... is equal to ... ones.



$$3 \times 26 = 60 + 18 = 78$$

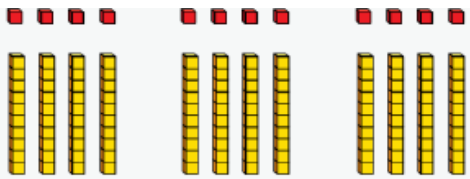
Part-whole models



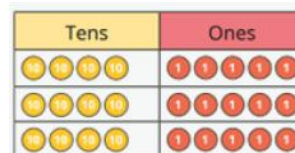
$$3 \times 26 = 78$$

Multiply a 2 or 3-digit number by a 1-digit number

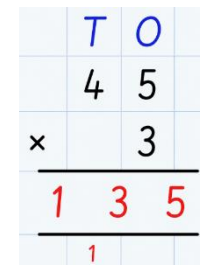
Base 10 or place-value counters arranged into equal groups
 $44 \times 3 =$



Formal method – short multiplication (using representations, such as place value grid/counters, to support)



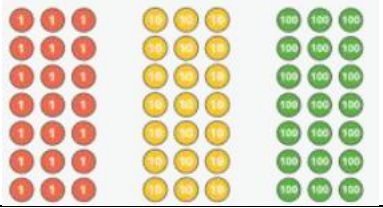
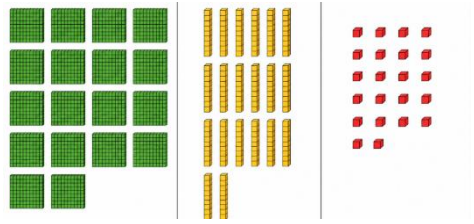
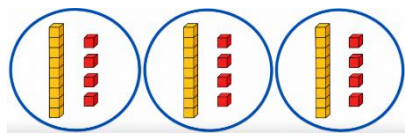
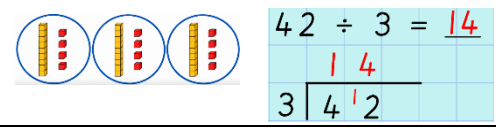
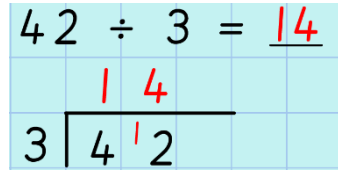
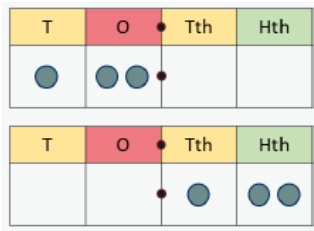
Short multiplication



Year 4 Division

Key Vocabulary:

commutative, inverse, multiple, product, remainder, scaling, factor, factor pair, inverse, triple, efficient

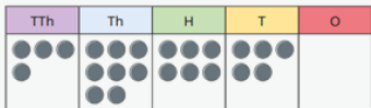
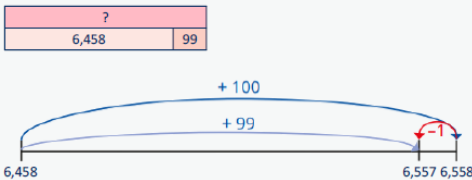
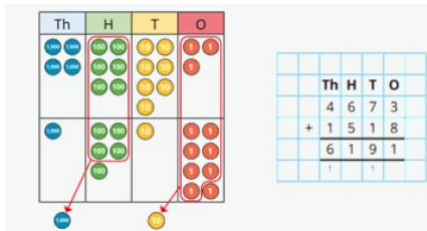
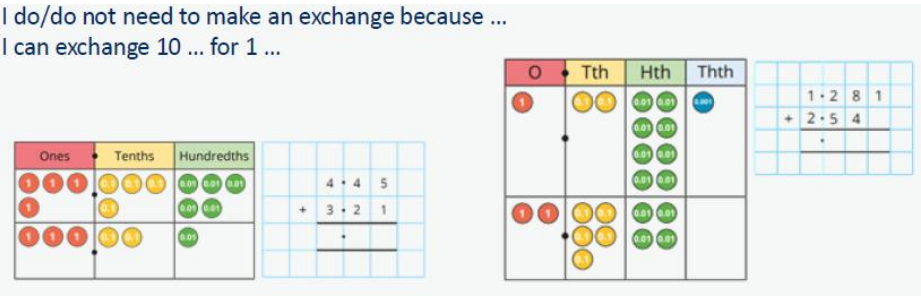
Progression of Skills	Concrete	Pictorial	Abstract
Related facts Link to known times-table facts	Base 10, place value counters ... ÷ ... is equal to ..., So ... tens ÷ ... is equal to ... tens. And ... hundreds ÷ is equal to ... hundreds. 	Use/draw representations of base 10/place value counters 	$21 \div 7 = 3$ $210 \div 7 = 30$ $2,100 \div 7 = 300$
Divide a 2 or 3-digit number by a 1-digit number	Base 10 or place-value counters arranged into equal groups 	Formal method – bus stop (using representations, such as place value grid/counters, to support) 	Bus stop (short division) 
Divide by 10 and 100	Place value grid & counters When I divide by 10/100, the digits move... place value column to the right. ... is one-tenth/one-hundredth the size of ... 	Use representations/drawings of place value grid & counters 	$12 \div 10 = 1.2$ $12 \div 100 = 0.12$

YEAR 5

Year 5 Addition

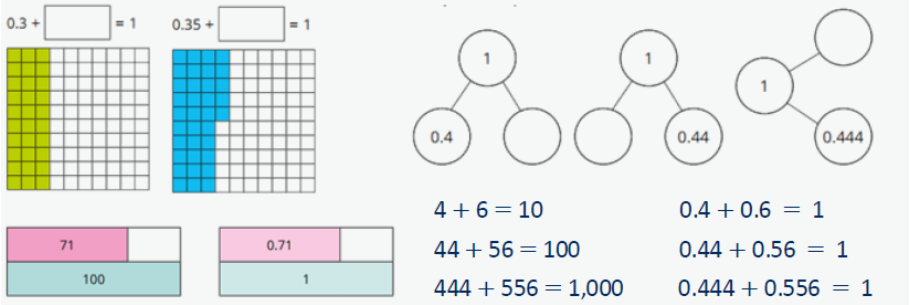
Key Vocabulary:

column, addition, digit, estimate, exchange, hundred(s), crossing the 10, crossing the 100, efficient, inverse, round, thousand(s), accurate, approximate, constant difference, strategy

Progression of Skills	Concrete	Pictorial	Abstract
Add using mental strategies Add 1s, 10s, 100s etc to any number. Use number bonds and related facts.	Place value chart  $48,650 + 300 =$ $48,650 + 30,000 =$ $48,650 + 30 =$	Numberlines, bar models To add..., I can add ... then subtract ... 	$6458 + 99 = 6558$
Add whole numbers with more than 4 digits	Base 10/place-value counters I can exchange 10 ... for 1 ... Formal method – column addition value grid/counters, to support) $4673 + 1518 = 6191$  (using representations, such as place		
Add decimals with up to 2 decimal places	I do/do not need to make an exchange because ... I can exchange 10 ... for 1 ... 		

Complements to 1

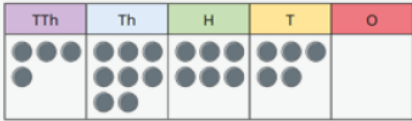
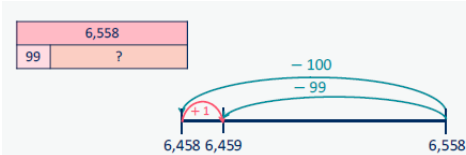
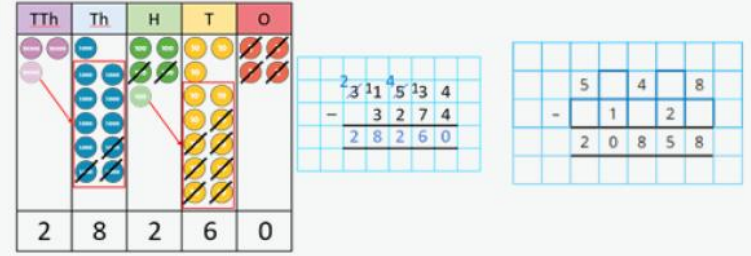
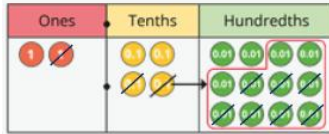
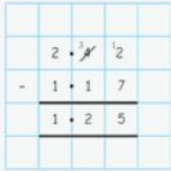
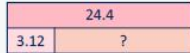
Pairs of numbers with up to 3 decimal places which total 1



Year 5 Subtraction

Key Vocabulary:

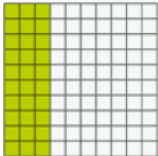
column, subtraction, digit, estimate, exchange, hundred(s), crossing the 10, crossing the 100, efficient, inverse, round, thousand(s), accurate, approximate, constant difference, strategy

Progression of Skills	Concrete	Pictorial	Abstract
Subtract using mental strategies Add 1s, 10s, 100s etc to any number. Use number bonds and related facts.	Place value chart  $48,650 - 300 =$ $48,650 - 30,000 =$ $48,650 - 30 =$	Numberlines, bar models To subtract..., I can subtract ... then add ... 	$6558 - 99 = 6459$
Subtract whole numbers with more than 4 digits	Base 10/place-value counters I can exchange 1 ... for 10 ... Formal method – column subtraction (using representations, such as place value grid/counters, to support) $31534 - 3274 = 28260$ 		
Subtract decimals with up to 2 decimal places	    		

Complements to 1

Pairs of numbers with up to 3 decimal places which total 1

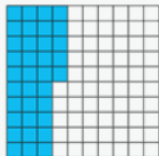
$0.3 + \square = 1$



10	
3	?

1	
0.3	?

$0.35 + \square = 1$



100	
35	?

1	
0.35	?

1

0.4

1

0.44

1

0.444

$10 - 4 = 6$

$100 - 44 = 56$

$1,000 - 444 = 556$

$1 - 0.4 = 0.6$

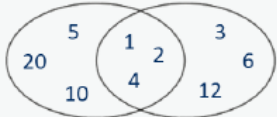
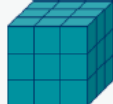
$1 - 0.44 = 0.56$

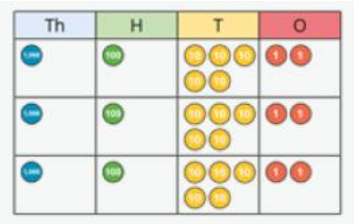
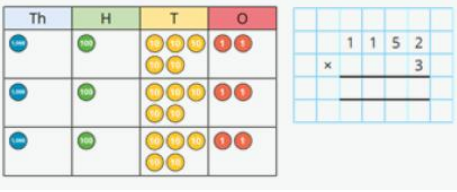
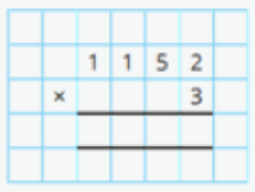
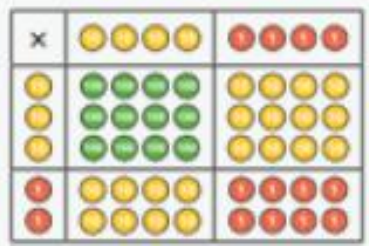
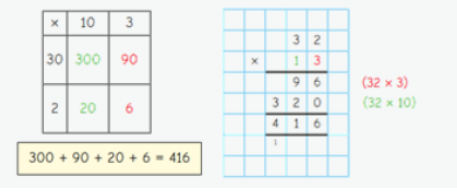
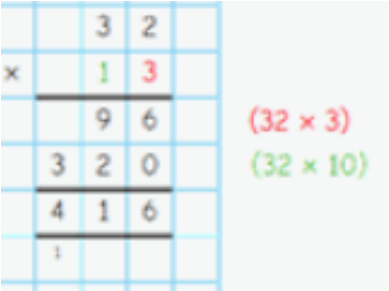
$1 - 0.444 = 0.556$

Year 5 Multiplication

Key Vocabulary:

commutative, inverse, multiple, product, remainder, scaling, factor, factor pair, inverse, triple, efficient, common multiple, common factor, cube number, prime number, square number

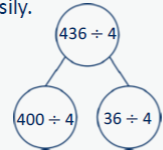
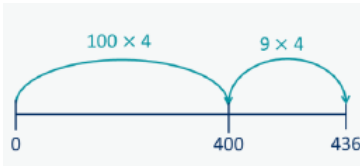
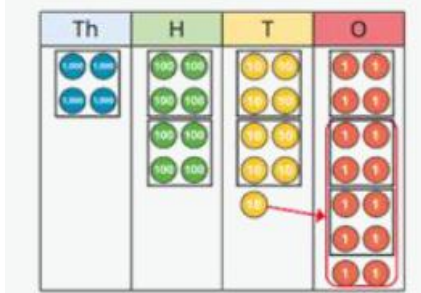
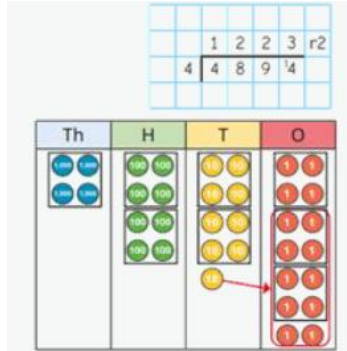
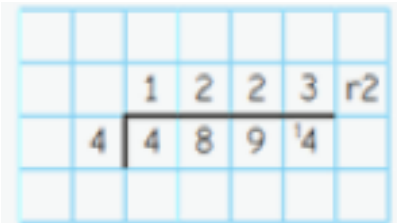
Progression of Skills	Concrete	Pictorial	Abstract																																																				
Multiples and Factors	... is a multiple of ... because ... × ... = ...  <table border="1" data-bbox="739 569 1104 678"><tr><td>1</td><td>2</td><td>3</td><td>4</td><td>5</td><td>6</td><td>7</td><td>8</td><td>9</td><td>10</td></tr><tr><td>11</td><td>12</td><td>13</td><td>14</td><td>15</td><td>16</td><td>17</td><td>18</td><td>19</td><td>20</td></tr><tr><td>21</td><td>22</td><td>23</td><td>24</td><td>25</td><td>26</td><td>27</td><td>28</td><td>29</td><td>30</td></tr></table>	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	... is a factor of ... because ... × ... = ...  1 × 8  2 × 4 1, 2, 4 and 8 are factors of 8	The common factors of ... and ... are ... Factors of 20 Factors of 12 																						
1	2	3	4	5	6	7	8	9	10																																														
11	12	13	14	15	16	17	18	19	20																																														
21	22	23	24	25	26	27	28	29	30																																														
Square and Cube numbers	... squared means ... × ...  1 × 1 1² = 1  2 × 2 2² = 4  3 × 3 3² = 9  4 × 4 4² = 16	... cubed means ... × ... × ...  1 × 1 × 1 1³ = 1  2 × 2 × 2 2³ = 8  3 × 3 × 3 3³ = 27																																																					
Multiply by 10, 100 and 1000	Place value grid & counters When I multiply by 10/100/1000, the digits move... place value column to the left. ... is 10/100/1000 times the size of ... <table border="1" data-bbox="616 1181 862 1228"><tr><td>M</td><td>HTh</td><td>TTh</td><td>Th</td><td>H</td><td>T</td><td>O</td></tr><tr><td></td><td></td><td></td><td></td><td>2</td><td>3</td><td>4</td></tr></table> 234 × 10 = 2,340 234 × 100 = 23,400 234 × 1,000 = 234,000 <table border="1" data-bbox="893 1181 1104 1228"><tr><td>Th</td><td>H</td><td>T</td><td>O</td><td>TTh</td><td>HTh</td></tr><tr><td></td><td></td><td></td><td>2</td><td>3</td><td>4</td></tr></table> 2.34 × 10 = 23.4 2.34 × 100 = 234 2.34 × 1,000 = 2,340	M	HTh	TTh	Th	H	T	O					2	3	4	Th	H	T	O	TTh	HTh				2	3	4	Use representations/drawings of place value grid & counters <table border="1" data-bbox="1128 1093 1377 1141"><tr><td>M</td><td>HTh</td><td>TTh</td><td>Th</td><td>H</td><td>T</td><td>O</td></tr><tr><td></td><td></td><td></td><td></td><td>2</td><td>3</td><td>4</td></tr></table> <table border="1" data-bbox="1411 1093 1619 1141"><tr><td>Th</td><td>H</td><td>T</td><td>O</td><td>TTh</td><td>HTh</td></tr><tr><td></td><td></td><td></td><td>2</td><td>3</td><td>4</td></tr></table>	M	HTh	TTh	Th	H	T	O					2	3	4	Th	H	T	O	TTh	HTh				2	3	4	234 × 10 = 2340 234 × 100 = 23,400 234 × 1000 = 234,000 2.34 × 10 = 23.4 2.34 × 100 = 234 2.34 × 1000 = 2340
M	HTh	TTh	Th	H	T	O																																																	
				2	3	4																																																	
Th	H	T	O	TTh	HTh																																																		
			2	3	4																																																		
M	HTh	TTh	Th	H	T	O																																																	
				2	3	4																																																	
Th	H	T	O	TTh	HTh																																																		
			2	3	4																																																		

Mental strategies Partition 2 or 3-digit numbers to multiply using informal methods.	The most efficient strategy to calculate ... $\times$... is ... To calculate ... $\times$ 12, I can do ... $\times$... $\times$... For example: 121×12 I could calculate 100×12 plus 20×12 plus 1×12 I could calculate 121×10 plus 121×2 I could calculate $121 \times 6 \times 2$ I could calculate $121 \times 4 \times 3$		
Multiply numbers up to 4 digits by a 1-digit number	Place-value counters 	Formal method – short multiplication (using representations, such as place value grid/counters, to support) 	Short multiplication $1152 \times 3 =$ 
Multiply numbers up to 4 digits by a 2-digit number	Place-value counters 	Formal method – Long multiplication (using representations to support) First, I multiply by the ... Then I multiply by the ... 	
			Long multiplication $32 \times 13 = 416$ 

Year 5 Division

Key Vocabulary:

commutative, inverse, multiple, product, remainder, scaling, factor, factor pair, inverse, triple, efficient, common multiple, common factor, cube number, prime number, square number

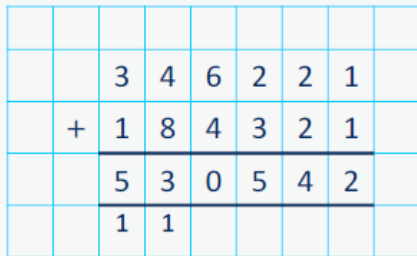
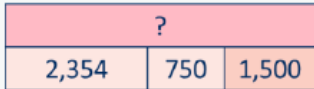
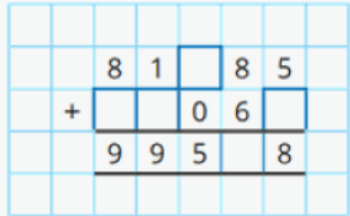
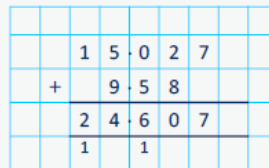
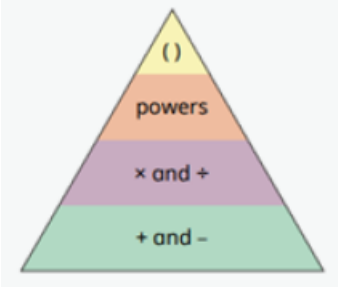
Progression of Skills	Concrete	Pictorial	Abstract
Mental strategies	Part whole models, numberlines I can partition ... into ... and ... to help me to divide more easily.  		To divide by ..., I can divide by ... and then divide the result by ... $436 \div 4 = 436 \div 2 \div 2$ $436 \div 2 = 218$ $218 \div 2 = 109$
Divide numbers up to 4 digits by a 1-digit number	Base 10 or place-value counters 	Formal method – bus stop (using representations, such as place value grid/counters, to support) 	Bus stop (short division) $4894 \div 4 = 1223 \text{ r}2$ 
Divide by 10, 100 and 1000	Place value grid & counters When I divide by 10/100/1000, the digits move... place value column to the right. ... is one-tenth/one-hundredth/one-thousandth the size of ...	 $120 \div 10 = 12$ $120 \div 100 = 1.2$ $120 \div 1,000 = 0.12$	$120 \div 10 = 12$ $120 \div 100 = 1.2$ $120 \div 1000 = 0.12$

YEAR 6

Year 6 Addition

Key Vocabulary:

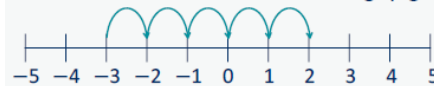
column, addition, digit, estimate, exchange, hundred(s), crossing the 10, crossing the 100, efficient, inverse, round, thousand(s), accurate, approximate, constant difference, strategy, order of operations

Progression of Skills	Concrete	Pictorial	Abstract												
Add integers up to 10 million															
Add decimals with up to 3 decimal places	I do/do not need to make an exchange because ... 														
Order of operations		Order of Operations <table><tr><td>B Brackets</td><td>$10 \times (4 + 2) = 10 \times 6 = 60$</td></tr><tr><td>O Order</td><td>$5 + 2^2 = 5 + 4 = 9$</td></tr><tr><td>D Division</td><td>$10 + 6 \div 2 = 10 + 3 = 13$</td></tr><tr><td>M Multiplication</td><td>$10 - 4 \times 2 = 10 - 8 = 2$</td></tr><tr><td>A Addition</td><td>$10 \times 4 + 7 = 40 + 7 = 47$</td></tr><tr><td>S Subtraction</td><td>$10 \div 2 - 3 = 5 - 3 = 2$</td></tr></table>	B Brackets	$10 \times (4 + 2) = 10 \times 6 = 60$	O Order	$5 + 2^2 = 5 + 4 = 9$	D Division	$10 + 6 \div 2 = 10 + 3 = 13$	M Multiplication	$10 - 4 \times 2 = 10 - 8 = 2$	A Addition	$10 \times 4 + 7 = 40 + 7 = 47$	S Subtraction	$10 \div 2 - 3 = 5 - 3 = 2$	
B Brackets	$10 \times (4 + 2) = 10 \times 6 = 60$														
O Order	$5 + 2^2 = 5 + 4 = 9$														
D Division	$10 + 6 \div 2 = 10 + 3 = 13$														
M Multiplication	$10 - 4 \times 2 = 10 - 8 = 2$														
A Addition	$10 \times 4 + 7 = 40 + 7 = 47$														
S Subtraction	$10 \div 2 - 3 = 5 - 3 = 2$														

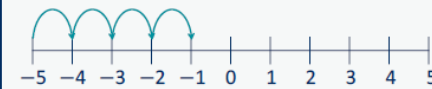
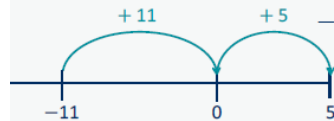
Negative numbers

... plus ... is equal to ...

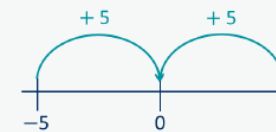
$$-3 + 5 = 2$$



$$-11 + 16 = 5$$



The difference between -5 and -1 is 4

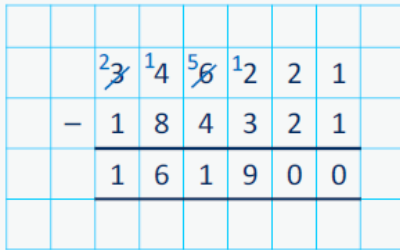
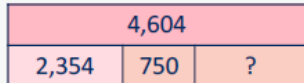
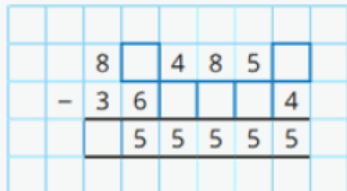
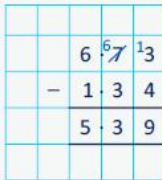
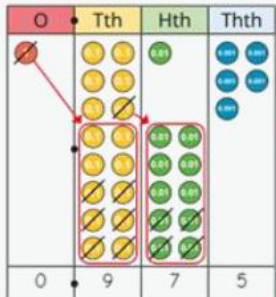
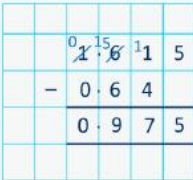
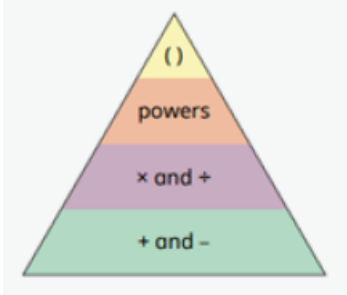


The difference between -5 and 5 is 10

Year 6 Subtraction

Key Vocabulary:

column, subtraction, digit, estimate, exchange, hundred(s), crossing the 10, crossing the 100, efficient, inverse, round, thousand(s), accurate, approximate, constant difference, strategy, order of operations

Progression of Skills	Concrete	Pictorial	Abstract												
Subtract integers up to 10 million															
Subtract decimals with up to 3 decimal places	I do/do not need to make an exchange because ... 														
Order of operations		Order of Operations <table><tr><td>B Brackets</td><td>$10 \times (4 + 2) = 10 \times 6 = 60$</td></tr><tr><td>O Order</td><td>$5 + 2^2 = 5 + 4 = 9$</td></tr><tr><td>D Division</td><td>$10 + 6 \div 2 = 10 + 3 = 13$</td></tr><tr><td>M Multiplication</td><td>$10 - 4 \times 2 = 10 - 8 = 2$</td></tr><tr><td>A Addition</td><td>$10 \times 4 + 7 = 40 + 7 = 47$</td></tr><tr><td>S Subtraction</td><td>$10 \div 2 - 3 = 5 - 3 = 2$</td></tr></table>	B Brackets	$10 \times (4 + 2) = 10 \times 6 = 60$	O Order	$5 + 2^2 = 5 + 4 = 9$	D Division	$10 + 6 \div 2 = 10 + 3 = 13$	M Multiplication	$10 - 4 \times 2 = 10 - 8 = 2$	A Addition	$10 \times 4 + 7 = 40 + 7 = 47$	S Subtraction	$10 \div 2 - 3 = 5 - 3 = 2$	
B Brackets	$10 \times (4 + 2) = 10 \times 6 = 60$														
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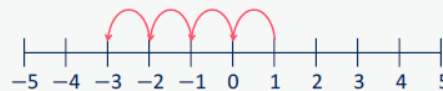
Negative numbers

... minus ... is equal to ...

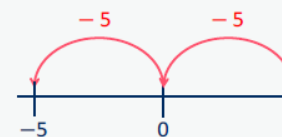
$$-1 - 4 = -5$$



$$1 - 4 = -3$$



The difference between -5 and -1 is 4



The difference between 5 and -5 is 10

Year 6 Multiplication

Key Vocabulary:

commutative, inverse, multiple, product, remainder, scaling, factor, factor pair, inverse, triple, efficient, common multiple, common factor, cube number, prime number, square number, composite number, order of operations, powers of

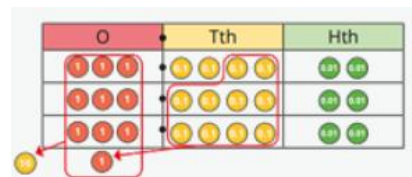
Progression of Skills	Concrete	Pictorial	Abstract																																																				
Multiply by 10, 100 and 1000	Place value grid & counters When I multiply by 10/100/1000, the digits move... place value column to the left. ... is 10/100/1000 times the size of ... <table><tr><td>M</td><td>HTh</td><td>TTh</td><td>Th</td><td>H</td><td>T</td><td>O</td></tr><tr><td></td><td></td><td></td><td></td><td>2</td><td>3</td><td>4</td></tr></table> <table><tr><td>Th</td><td>H</td><td>T</td><td>O</td><td>TTh</td><td>Hh</td></tr><tr><td></td><td></td><td></td><td></td><td>2</td><td>3</td></tr></table> $234 \times 10 = 2,340$ $234 \times 100 = 23,400$ $234 \times 1,000 = 234,000$ $2.34 \times 10 = 23.4$ $2.34 \times 100 = 234$ $2.34 \times 1,000 = 2,340$	M	HTh	TTh	Th	H	T	O					2	3	4	Th	H	T	O	TTh	Hh					2	3	Use representations/drawings of place value grid & counters <table><tr><td>M</td><td>HTh</td><td>TTh</td><td>Th</td><td>H</td><td>T</td><td>O</td></tr><tr><td></td><td></td><td></td><td></td><td>2</td><td>3</td><td>4</td></tr></table> <table><tr><td>Th</td><td>H</td><td>T</td><td>O</td><td>TTh</td><td>Hh</td></tr><tr><td></td><td></td><td></td><td></td><td>2</td><td>3</td></tr></table>	M	HTh	TTh	Th	H	T	O					2	3	4	Th	H	T	O	TTh	Hh					2	3	$234 \times 10 = 2340$ $234 \times 100 = 23,400$ $234 \times 1000 = 234,000$ $2.34 \times 10 = 23.4$ $2.34 \times 100 = 234$ $2.34 \times 1000 = 2340$
M	HTh	TTh	Th	H	T	O																																																	
				2	3	4																																																	
Th	H	T	O	TTh	Hh																																																		
				2	3																																																		
M	HTh	TTh	Th	H	T	O																																																	
				2	3	4																																																	
Th	H	T	O	TTh	Hh																																																		
				2	3																																																		
Multiply numbers up to 4 digits by a 2-digit number	Formal method – Long multiplication To multiply by a 2-digit number, first multiply by the ones, then multiply by the tens and then find the total. <table><tr><td></td><td></td><td></td><td></td><td></td><td></td></tr><tr><td></td><td></td><td>1</td><td>2</td><td>0</td><td>7</td></tr><tr><td></td><td>×</td><td></td><td></td><td>3</td><td>6</td></tr><tr><td>+</td><td></td><td>7</td><td>2</td><td>4</td><td>2</td></tr><tr><td></td><td>3</td><td>6</td><td>2</td><td>1</td><td>0</td></tr><tr><td></td><td>4</td><td>3</td><td>4</td><td>5</td><td>2</td></tr><tr><td></td><td>1</td><td></td><td></td><td></td><td></td></tr></table> (1,207 × 6) (1,207 × 30)											1	2	0	7		×			3	6	+		7	2	4	2		3	6	2	1	0		4	3	4	5	2		1														
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	4	3	4	5	2																																																		
	1																																																						
Order of operations	Order of Operations <table><tr><td>B</td><td>Brackets</td><td>$10 \times (4 + 2) = 10 \times 6 = 60$</td></tr><tr><td>O</td><td>Order</td><td>$5 + 2^2 = 5 + 4 = 9$</td></tr><tr><td>D</td><td>Division</td><td>$10 \div 6 \div 2 = 10 \div 3 = 13$</td></tr><tr><td>M</td><td>Multiplication</td><td>$10 - 4 \times 2 = 10 - 8 = 2$</td></tr><tr><td>A</td><td>Addition</td><td>$10 \times 4 + 7 = 40 + 7 = 47$</td></tr><tr><td>S</td><td>Subtraction</td><td>$10 \div 2 - 3 = 5 - 3 = 2$</td></tr></table>			B	Brackets	$10 \times (4 + 2) = 10 \times 6 = 60$	O	Order	$5 + 2^2 = 5 + 4 = 9$	D	Division	$10 \div 6 \div 2 = 10 \div 3 = 13$	M	Multiplication	$10 - 4 \times 2 = 10 - 8 = 2$	A	Addition	$10 \times 4 + 7 = 40 + 7 = 47$	S	Subtraction	$10 \div 2 - 3 = 5 - 3 = 2$																																		
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Multiply decimals by integers

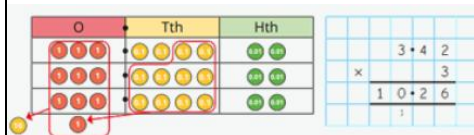
Place value counters

I know that ... x ... = ..., so I also know that ... x ... =

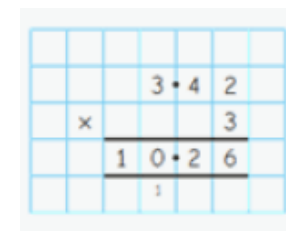
I need to exchange 10 ... for 1 ...



Formal method – short multiplication
(using representations, such as place value grid/counters, to support)



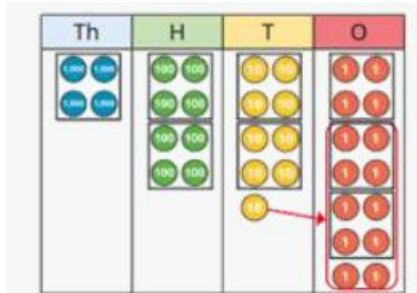
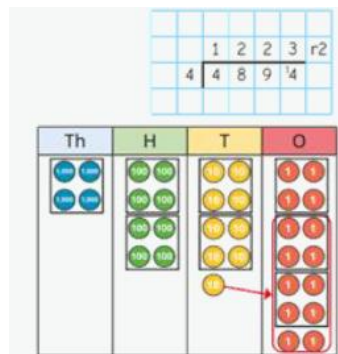
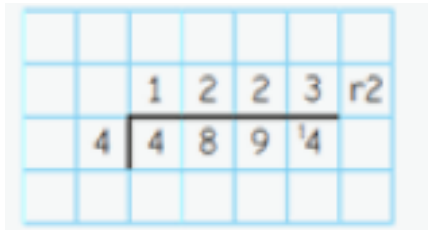
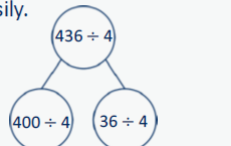
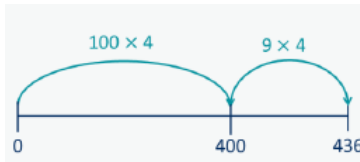
Short multiplication
 $3.42 \times 3 = 10.26$

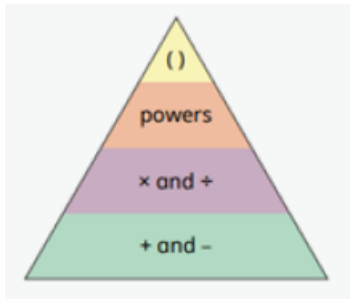
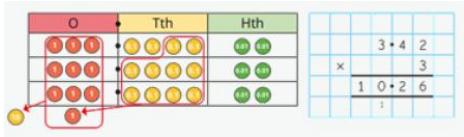
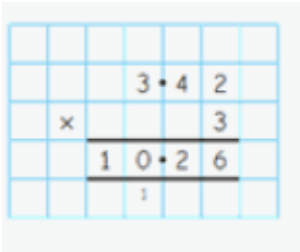


Year 6 Division

Key Vocabulary:

commutative, inverse, multiple, product, remainder, scaling, factor, factor pair, inverse, triple, efficient, common multiple, common factor, cube number, prime number, square number, composite number, order of operations, powers of

Progression of Skills	Concrete	Pictorial	Abstract
Divide by 10, 100 and 1000	Place value grid & counters When I divide by 10/100/1000, the digits move... place value column to the right. ... is one-tenth/one-hundredth/one-thousandth the size of ...	Th H T O Tth Hth ● ●● ● Th H T O Tth Hth ● ●● ● Th H T O Tth Hth ● ●● Th H T O Tth Hth ● ●● $120 \div 10 = 12$ $120 \div 100 = 1.2$ $120 \div 1,000 = 0.12$	$120 \div 10 = 12$ $120 \div 100 = 1.2$ $120 \div 1000 = 0.12$
Short division	Base 10 or place-value counters 	Formal method – bus stop (using representations, such as place value grid/counters, to support) 	Bus stop (short division) $4894 \div 4 = 1223 \text{ r}2$ 
Mental strategies	Part whole models, numberlines I can partition ... into ... and ... to help me to divide more easily.  	To divide by ..., I can divide by ... and then divide the result by ... $436 \div 4 = 436 \div 2 \div 2$ $436 \div 2 = 218$ $218 \div 2 = 109$	

Order of operations Calculations in brackets should be done first. Multiplication and division should be performed before addition and subtraction. *When no brackets re shown and the operations have the same priority, work left to right.		Order of Operations <table><tr><td>B</td><td>Brackets</td><td>$10 \times (4 + 2) = 10 \times 6 = 60$</td></tr><tr><td>O</td><td>Order</td><td>$5 + 2^2 = 5 + 4 = 9$</td></tr><tr><td>D</td><td>Division</td><td>$10 \div 6 \div 2 = 10 \div 3 = 13$</td></tr><tr><td>M</td><td>Multiplication</td><td>$10 - 4 \times 2 = 10 - 8 = 2$</td></tr><tr><td>A</td><td>Addition</td><td>$10 \times 4 + 7 = 40 + 7 = 47$</td></tr><tr><td>S</td><td>Subtraction</td><td>$10 \div 2 - 3 = 5 - 3 = 2$</td></tr></table>	B	Brackets	$10 \times (4 + 2) = 10 \times 6 = 60$	O	Order	$5 + 2^2 = 5 + 4 = 9$	D	Division	$10 \div 6 \div 2 = 10 \div 3 = 13$	M	Multiplication	$10 - 4 \times 2 = 10 - 8 = 2$	A	Addition	$10 \times 4 + 7 = 40 + 7 = 47$	S	Subtraction	$10 \div 2 - 3 = 5 - 3 = 2$
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Divide decimals by integers	Place value counters I know that ... ÷ ... = ..., so I also know that ... ÷ ... = I need to exchange 10 ... for 1 ... 	Formal method – Bus stop (using representations, such as place value grid/counters, to support) 	Bus stop (short division) 5.32 ÷ 4 = 1.33 																	

*For Calculations not included in this policy, e.g. Fractions, Percentages, Time etc, please see the White Rose Calculation Policy.